

MATH 2107-601

Take-Home Quiz 1

Due: Monday, February 5, 2001, 6:00 p.m. (Handed out: 1/29/2001)

NAME (Print): _____ Student I.D.: _____

NAME (Signature): _____

PART A: State whether the following statements are *true* (T) or *false* (F).

1. _____ $\lim_{x \rightarrow 0} 2 = 0.$

7. _____ $\lim_{x \rightarrow -\infty} \frac{x}{\sqrt{x^2-4}} = 1.$

2. _____ $\lim_{x \rightarrow -1} \frac{x^2+x}{x^2-1} = -\frac{1}{2}.$

3. _____ $\lim_{x \rightarrow 1} \frac{3x^2-6x+3}{x-1} = 0.$

8. _____ $\lim_{x \rightarrow 2^+} \sqrt{x-2} = 0.$

4. _____ $\lim_{x \rightarrow 2^{ss}} \frac{3-\sqrt{x+7}}{2-x} = 1.$

9. _____ $\lim_{x \rightarrow 2} \sqrt{x-2} = 0.$

5. _____ $\lim_{x \rightarrow a^+} (mx + b) = ma + b.$

10. _____ $\lim_{x \rightarrow 2^-} \sqrt{x-2}$ does *not* exist.

6. _____ $\lim_{x \rightarrow \infty} \frac{x}{\sqrt{x^2-4}} = 1.$

11. _____ $\lim_{x \rightarrow \infty} \frac{x^3}{x^2+1} = \infty.$

12. _____ To *prove* that $\lim_{x \rightarrow 2} (3x - 2) = 4$, we must show that , for *some* neighborhood $N = (4 - \epsilon, 4 + \epsilon)$ of 4, there is a deleted neighborhood $D = (2 - \delta, 2) \cup (2, 2 + \delta)$ of 2 such that for all x in D , $3x - 2$ is in N .

13. _____ To *prove* that $\lim_{x \rightarrow 2} (3x - 2) = 4$, we must show that , for *any given* neighborhood $N = (4 - \epsilon, 4 + \epsilon)$ of 4, there is a deleted neighborhood $D = (2 - \delta, 2) \cup (2, 2 + \delta)$ of 2 such that for all x in D , $3x - 2$ is in N .

14. _____ The function $f(x) = \frac{2}{x-3}$ can be made *continuous* at $x = 3$.

15. _____ The function $f(x) = \frac{2x^2 - 12x + 18}{x-3}$ can be made *continuous* at $x = 3$.

PART B: *Circle* the *one* correct choice.

1. $\lim_{x \rightarrow 3^+} \frac{|x-3|}{x-3}$ is

- a) 3
- b) 1
- c) 0
- d) -1
- e) none of the above

3. $\lim_{x \rightarrow 3} \frac{|x-3|}{x-3}$ is

- a) 3
- b) 1
- c) 0
- d) -1
- e) none of the above

2. $\lim_{x \rightarrow 3^-} \frac{|x-3|}{x-3}$ is

- a) 3
- b) 1
- c) 0
- d) -1
- e) none of the above

4. $\lim_{x \rightarrow +\infty} \frac{|x-3|}{x-3}$ is

- a) $+\infty$
- b) 1
- c) 0
- d) -1
- e) none of the above

5. $\lim_{x \rightarrow -\infty} \frac{|x-3|}{x-3}$ is
- a) 1
 - b) 0
 - c) -1
 - d) $-\infty$
 - e) none of the above
6. $\lim_{x \rightarrow -2} \frac{x^2-x-6}{x^2+3x+2}$
- a) does not exist
 - b) is 5
 - c) is 1
 - d) is 0
 - e) is -5
7. $\lim_{x \rightarrow a} \frac{x^2-a}{x-a^2}$, for $a \neq 0$ or $a \neq 1$,
- a) does not exist
 - b) is 0
 - c) is 1
 - d) is -1
 - e) is 2
8. $\lim_{x \rightarrow a} a$ is
- a) a^2
 - b) a
 - c) 0
 - d) 1
 - e) none of the above
9. If $f(x) = |x - 3|$, then $\lim_{x \rightarrow 3^+} \frac{f(x)-f(3)}{x-3}$ is
- a) 1
 - b) 0
 - c) -1
 - d) 3
 - e) none of the above
10. If $f(x) = |x - 3|$, then $\lim_{h \rightarrow 0^-} \frac{f(3+h)-f(3)}{h}$ is
- a) 1
 - b) 0
 - c) -1
 - d) 3
 - e) none of the above