

MATH 2107-601 EXAM #2 Study Guide NAME: \_\_\_\_\_  
(Print)

THURSDAY

November 16, 2006

NAME: \_\_\_\_\_  
(Signature)

[6:30 p.m. - 7:45 p.m.]

STUDENT I. D.: \_\_\_\_\_

**INSTRUCTIONS:** There are 2 parts to this exam, the main part plus an optional **EXTRA CREDIT** part (on the last page). The main part is worth 100 points while the extra credit part is worth 12 points. But any score over 100 will be truncated to 100.

Clarity of exposition (including proper spelling and punctuation is an integral part of a correct solution to any problem. In particular, **DO NOT PUT EQUAL SIGNS BETWEEN THINGS THAT ARE NOT EQUAL**. But do put them where they belong.

It is necessary to show all your work.

**NOTE:** EXAM #2 will be given on Tuesday, November 21, 2006.

**GOOD LUCK!**

---

**PLEASE SIGN THE FOLLOWING STATEMENT:**

On my honor, I declare that the work that follows is entirely my own. With regard to all the questions on this exam, I have neither given nor received help from anyone [including myself, say, via any type of cheat sheet or device (e.g., cell phone)]. Nor have I used a calculator of any sort (i.e., regular or programmable).

NAME: \_\_\_\_\_  
(Signature)

---

PLEASE DO NOT WRITE BELOW THIS LINE:

---

1. a. \_\_\_\_\_

b. \_\_\_\_\_

2. a. \_\_\_\_\_

b. \_\_\_\_\_

3. \_\_\_\_\_

4. a. \_\_\_\_\_

b. \_\_\_\_\_

c. \_\_\_\_\_

d. \_\_\_\_\_

Total: \_\_\_\_\_

5. a. \_\_\_\_\_

b. \_\_\_\_\_

c. \_\_\_\_\_

d. \_\_\_\_\_

e. \_\_\_\_\_

f. \_\_\_\_\_

g. \_\_\_\_\_

h. \_\_\_\_\_

Total: \_\_\_\_\_

EXTRA-CREDIT:

1. \_\_\_\_\_

2. \_\_\_\_\_

TOTALS:

Column 3: \_\_\_\_\_

Column 2: \_\_\_\_\_

Column 1: \_\_\_\_\_

Grand Total: \_\_\_\_\_

Grade: \_\_\_\_\_

1. (a) Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be a function and let  $a \in \mathbb{R}$ . Prove that  $f$  is continuous at  $a$  whenever  $f'(a)$  exists.

[10 points]

- (b) Give an example of a function  $f : \mathbb{R} \rightarrow \mathbb{R}$  and a point  $a \in \mathbb{R}$  such that  $f$  is continuous at  $a$  but  $f'(a)$  does not exist.

[To get credit, you must give at least some indication of why  $f$  is continuous at  $a$  and why  $f'(a)$  does not exist.]

[5 points]

2. (a) State the Chain Rule. Be sure to state the hypotheses as well as the conclusion.

ANSWER:

The Chain Rule:

Hypotheses:

[1 point]

Conclusions:

[4 points]

- (b) Complete the following:

[5 points: 1 each]

$$(F \cdot S)' =$$

$$\left(\frac{T}{B}\right)' =$$

$$(c \cdot F)' =$$

$$(F + G)' =$$

$$(F^n)' =$$

3. Assume that the equation

$$x^4 + x^3y^3 + y^4 = 1$$

defines  $y$  as a differentiable function of  $x$ . Use implicit differentiation

to find  $\frac{dy}{dx}$ . Then find the equation of the straight line tangent to

the graph of  $x^4 + x^3y^3 + y^4 = 1$  at the point  $(1, -1)$ .

[15 points]

**SOLUTION:**

4. For each of the following, use the various rules that we have developed [not the definition] to compute  $f'(x)$  when  $f(x)$  is given.

Then **SIMPLIFY** your answers as much as possible.

**NOTE:** DO NOT COMPUTE  $f'(x)$  DIRECTLY FROM THE DEFINITION!

[20 points: 5 each]

a.  $f(x) = \frac{x^3}{x^3 + 1}$

b.  $f(x) = \left(\frac{x^4 - 1}{x^4 + 1}\right)^5$

c.  $f(x) = \frac{\cos x}{1 - \sin x}$

d.  $f(x) = \frac{1 - \sin x}{\cos x}$

5. (Continued):

e.  $f(x) = 5^{(x^3 + 3x + 2)}$

f.  $f(x) = e^{x^{16}} \cdot \csc(x^4)$

g.  $f(x) = \sec(x^6) \cdot \cot(6^x)$

h.  $f(x) = \frac{(3x + 4) \cdot \sqrt{5x + 6}}{2x^2 + 3x + 4}$  [Use logarithmic differentiation.]

**EXTRA-CREDIT:** Circle the *one* correct choice.

[12 points : But, any exam score over 100 will be truncated to 100.]

For each of the following, use the various rules that we have developed

[not the definition] to compute  $f'(x)$  when  $f(x)$  is given.

Do **NOT** simplify your answers.

**NOTE:** DO NOT COMPUTE  $f'(x)$  DIRECTLY FROM THE

DEFINITION!

a.  $f(x) = [\sin^4 x]^{\tan x}$

[8 points]

b.  $f(x) = \log_7(7^{x^4}) + \log_7(x)$

[4 points]