

PROB# 4.16

Assume beam wt = 500#/ft

$$w_u = (1.2)(3.5) + (1.6)(1) = 5.80 \text{ k/ft}$$

$$M_u = (5.80)(12)(6) = 417.6 \text{ ft-k}$$

$$\rho = \frac{0.18 f'_c}{f_y} = \frac{(0.18)(4)}{60} = 0.012$$

$$\frac{M_u}{\phi b d^2} = 643.5 \text{ from Appendix Table A.13}$$

$$b d^2 = \frac{M_u}{\phi 643.5} = \frac{(12)(417,600)}{(0.9)(643.5)}$$

$$= 8653 \quad \left\{ \begin{array}{l} 14 \times 24.86 \\ 16 \times 23.25 \leftarrow \\ 18 \times 21.92 \end{array} \right.$$

USE 16 x 26 beam (d = 23.5 in.)

$$\text{Beam wt} = \frac{(16)(26)}{144} (150) = 433 \text{ \#/ft} < 500 \text{ \#/ft} \quad \underline{\text{OK}}$$

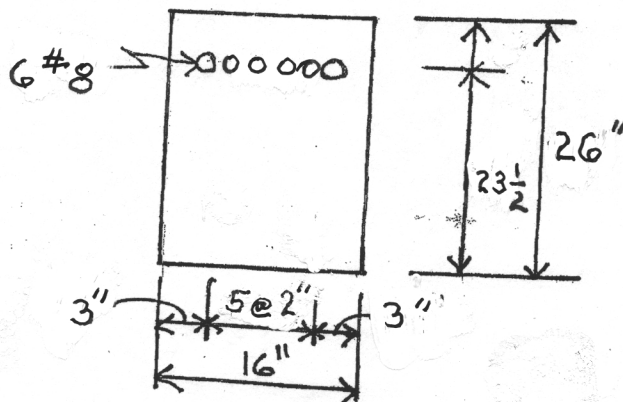
$$A_s = \rho b d = (0.012)(16)(23.5) = 4.51 \text{ in}^2$$

USE 6 #8 Bars (4.71 in<sup>2</sup>),  $b_{\min} = 15.3" < 16"$   
OK

$$\rho = \frac{A_s}{b d} = \frac{4.71}{(16)(23.5)} = 0.0125$$

>  $\rho_{\min} = 0.0033$  and  $< \rho_{\max} = 0.0181$  from App. Table A.7  
∴ Bm. is ductile &  $\phi = 0.9$

BEAM Cross Section



✓ JCM

PROB # 4.20

Assume beam wt = 950 #/ft

$$w_u = (1.2)(2.95) = 3.54 \text{ k/ft}$$

$$M_u = (3.54)(16)^2/2 + (1.6)(30)(8) + (1.6)(20)(16) = 1349 \text{ ft-k}$$

$$e = \frac{1}{2} e_{\max} = \left(\frac{1}{2}\right)(0.0181) = 0.00905$$

$$\frac{M_u}{\phi b d^2} = 499.5 \text{ from Appendix Table A.13}$$

$$b d^2 = \frac{M_u}{\phi 499.5} = \frac{(12)(1349000)}{(0.9)(499.5)}$$

$$= 36012 \begin{cases} 18 \times 44.72 \\ 20 \times 42.43 \\ 22 \times 40.45 \end{cases}$$

Use 20x45 beam (d = 42.50 in.)

$$\text{Beam wt} = \frac{(20)(45)}{144} (150) = 938 \text{ #/ft} < 950 \text{ #/ft} \quad \underline{\text{OK}}$$

$$A_s = \rho b d = (0.00905)(20)(42.5) = 7.69 \text{ in.}^2$$

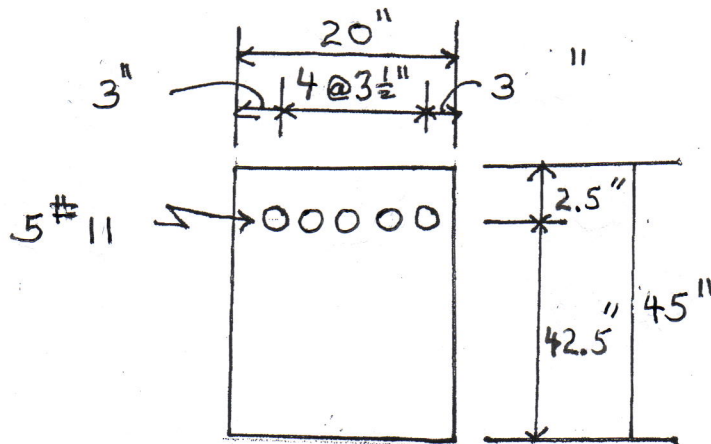
Use 5 #11 bars (7.81 in.<sup>2</sup>),  $b_{\min} = 16.6" < 20"$  OK

$$\rho = \frac{A_s}{b d} = \frac{7.81}{(20)(42.5)} = 0.00919$$

$$\rho > \rho_{\min} = 0.0033 < \rho_{\max} = 0.0181 \quad (\text{Table A.7})$$

$\therefore$  section is ductile and  $\phi = 0.9$

Sketch of Beam Cross Section



PROB # 4.26

Assume 7½-in. slab (d = 6¼ in.)

$$D = \frac{7.5}{12} (150) = 93.75 \#/\text{ft}$$

$$w_u = (1.2)(93.75) + (1.6)(150) = 352.5 \#/\text{ft}$$

$$M_u = \frac{(0.353)(24)^2}{8} = 25.38 \text{ ft-k}$$

$$\rho = \frac{1}{2} \rho_b = \left(\frac{1}{2}\right)(0.0285) = 0.01425$$

$$\frac{M_u}{\phi b d^2} = 747.15 \text{ from Appendix Table A.13}$$

$$d = \sqrt{\frac{(12)(25,380)}{(0.90)(12)(747.15)}} = 6.14 \text{ in.}$$

USE 7½-in. slab (d = 6.25 in.)

$$\frac{M_u}{\phi b d^2} = \frac{(12)(25,380)}{(0.90)(12)(6.25)^2} = 721.9$$

$$\rho = 0.0137 \text{ from Appendix Table A.13}$$

$$A_s = \rho b d = (0.0137)(12)(6.25) = 1.03 \text{ in.}^2/\text{ft}$$

USE #8 @ 9 in. (1.05 in.²/ft)

Shrinkage and temperature A<sub>s</sub>

$$A_s = (0.0018)(12)(7.5) = 0.162 \text{ in.}^2/\text{ft}$$

USE #3 @ 8 in. (0.17 in.²/ft)

*JCM*

PROB # 4.30

(a) Moment @ base of stem

$$M_u = (1.6) \left( \frac{1}{2} \times 500 \right) \left( 18 \times \frac{18}{3} \right) = 43,200 \text{ ft-lbs}$$

$$e = \frac{1}{2} p_b = 0.5 (0.0285) = 0.01425$$

$$\frac{M_u}{\phi b d^2} = 749.4 \text{ from Appendix Table A.13}$$

$$b d^2 = \frac{(12)(43,200)}{(0.9)(749.4)} = 768.6 \text{ in}^3$$

$$d = \sqrt{\frac{768.6}{b}} = \sqrt{\frac{768.6}{12}} = 8.00 \text{ in.}$$

(b) Use 11 in. thick wall (d = 8.50 in.)

$$A_s = \rho b d = (0.01425)(12)(8.5) = 1.45 \text{ in}^2/\text{ft}$$

USE #8 bars 6½ in. O.C. (1.45 in.²) Table A.6

$$\rho = \frac{1.45}{(12)(8.5)} = 0.0142$$

$$7\rho_{\min} = 0.0033 < \rho_{\max} = 0.0181$$

from Appendix Table A.7

∴ Stem is ductile and  $\phi = 0.9$

VJCM