



Standard Test Method for Inplane Shear Properties of Hoop Wound Polymer Matrix Composite Cylinders¹

This standard is issued under the fixed designation D 5448/D 5448M; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ϵ) indicates an editorial change since the last revision or reapproval.

1. Scope

1.1 This test method determines the inplane shear properties of wound polymer matrix composites reinforced by high-modulus continuous fibers. It describes testing of hoop wound (90°) cylinders in torsion for determination of inplane shear properties.

1.2 The values stated in either SI units or inch-pound units are to be regarded separately as standard. Within the text the inch-pound units are shown in brackets. The values stated in each system are not exact equivalents; therefore, each system must be used independently of the other. Combining values from the two systems may result in nonconformance with the test method.

1.3 *This standard does not purport to address all of the safety problems, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.*

2. Referenced Documents

2.1 ASTM Standards:

- D 792 Test Methods for Density and Specific Gravity (Relative Density) of Plastics by Displacement²
- D 883 Terminology Relating to Plastics²
- D 2584 Test Method for Ignition Loss of Cured Reinforced Resins³
- D 2734 Test Method for Void Content of Reinforced Plastics³
- D 3171 Test Method for Constituent Content of Composite Materials⁴
- D 3878 Terminology for Composite Materials⁴
- D 5229/D 5229M Test Method for Moisture Absorption Properties and Equilibrium Conditioning of Polymer Matrix Composite Materials⁴
- D 5449/D 5449M Test Method for Transverse Compressive

Properties of Hoop Wound Polymer Matrix Composite Cylinders⁴

D 5450/D 5450M Test Method for Transverse Tensile Properties of Hoop Wound Polymer Matrix Composite Cylinders⁴

E 4 Practices for Force Verification of Testing Machines⁵

E 6 Terminology Relating to Methods of Mechanical Testing⁵

E 111 Test Method for Young's Modulus, Tangent Modulus, and Chord Modulus⁵

E 122 Practice for Calculating Sample Size to Estimate with a Specified Tolerable Error, the Average for a Characteristic of a Lot or Process⁶

E 177 Practice for Use of the Terms Precision and Bias in ASTM Test Methods⁶

E 251 Test Methods for Performance Characteristics of Metallic Bonded Resistance Strain Gages⁵

E 456 Terminology Relating to Quality and Statistics⁶

E 691 Practice for Conducting and Interlaboratory Study to Determine the Precision of a Test Method⁶

E 1237 Guide for Installing Bonded Resistance Strain Gages⁵

3. Terminology

3.1 *Definitions*—Terminology D 3878 defines terms relating to high-modulus fibers and their composites. Terminology D 883 defines terms relating to plastics. Terminology E 6 defines terms relating to mechanical testing. Terminology E 456 and Practice E 177 define terms relating to statistics. In the event of a conflict between terms, Terminology D 3878 shall have precedence over other standards.

3.2 *Description of Terms Specific to This Standard:*⁷

3.2.1 *hoop wound, n*—a winding of a cylindrical component where the filaments are circumferentially oriented.

¹ This test method is under the jurisdiction of ASTM Committee D30 on High Modulus Fibers and Their Composites and is the direct responsibility of Subcommittee D30.04 on Lamina and Laminate Test Methods.

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² *Annual Book of ASTM Standards*, Vol 08.01.

³ *Annual Book of ASTM Standards*, Vol 08.02.

⁴ *Annual Book of ASTM Standards*, Vol 15.03.

⁵ *Annual Book of ASTM Standards*, Vol 03.01.

⁶ *Annual Book of ASTM Standards*, Vol 14.02.

⁷ If the term represents a physical quantity, its analytical dimensions are stated immediately following the term (or letter symbol) in fundamental dimension form, using the following ASTM standard symbology for fundamental dimensions, shown within square brackets: [M] for mass, [L] for length, [T] for time, [θ] for thermodynamic temperature, and [nd] for nondimensional quantities. Use of these symbols is restricted to analytical dimensions when used with square brackets, as the symbols may have other definitions when used without the brackets.

3.2.2 *inplane shear modulus*, G_{12} [$MT^{-1}T^{-2}$], n —the elastic shear modulus of a unidirectional material in the plane defined by axes parallel and perpendicular to the reinforcing fibers.

3.2.3 *inplane shear strain at failure*, γ_{12}^u [nd], n —the value of inplane shear strain at failure when an inplane shear load is applied to the material.

3.2.4 *inplane shear strength*, τ_{12} , [$MT^{-2}L^{-1}$], n —the strength of a unidirectional material when an inplane shear load is applied to the material.

3.2.5 *specimen*—a single part cut from a winding that meets the specifications of Fig. 1. Each winding may yield several specimens.

3.2.6 *winding*—an entire part completed by one winding operation and then cured.

4. Summary of Test Method

4.1 A thin walled hoop wound cylinder nominally 100 mm [4 in.] in diameter and 140 mm [5½ in.] in length is bonded into two end fixtures. The specimen/fixture assembly is mounted in the testing machine and monotonically loaded in inplane shear while recording load. The inplane shear strength can be determined from the maximum load carried prior to failure. If the cylinder strain is monitored with strain gages then the stress-strain response, the inplane shear strain at failure, and the inplane shear modulus can be derived.

5. Significance and Use

5.1 This test method is designed to produce inplane shear property data for material specifications, research and development, quality assurance, and structural design and analysis. Factors that influence the inplane shear response and should therefore be reported are material, method of material preparation, specimen preparation, specimen conditioning, environment of testing, specimen alignment and gripping, speed of testing, void content, and fiber volume fraction. Properties, in the test direction, that may be obtained from this test method are as follows:

- 5.1.1 *Inplane Shear Strength*, τ_{12}^u ,
- 5.1.2 *Inplane Shear Strain at Failure*, γ_{12}^u , and
- 5.1.3 *Inplane Shear Modulus*, G_{12} .

6. Interferences

6.1 *Material and Specimen Preparation*—Poor material fabrication practices, lack of control of fiber alignment, and damage induced by improper coupon machining are known causes of high material data scatter in composites.

6.2 *Bonding Specimens to Test Fixtures*—A high percentage of failures in or near the bond between the test specimen and the test fixture, especially when combined with high material data scatter, is an indicator of specimen bonding problems. Specimen-to-fixture bonding is discussed in 11.5.

6.3 *System Alignment*—Excessive bending or axial loading will cause premature failure, as well as highly inaccurate shear modulus determination. Every effort should be made to eliminate excess bending and axial loading from the test system. Bending and axial loading may occur due to misaligned grips, misaligned specimens in the test fixtures, or from departures of the specimens from tolerance requirements. The alignment should always be checked as discussed in 12.2.

7. Apparatus

7.1 *Micrometers*, suitable ball type for reading to within 0.025 ± 0.010 mm [0.001 ± 0.0004 in.] of the specimen inner and outer diameters. Flat anvil type or micrometer calipers of similar resolution may be used for the overall specimen length and the gage length (the free length between the fixtures).

7.2 *Inplane Shear Fixture*—The inplane shear fixture consists of a steel outer shell, insert, and adaptor. An assembly drawing for these components and the test fixture is shown in Fig. 1.

7.2.1 *Outer Shell*—The outer shell (SI units, see Fig. 2; inch-pound units, see Fig. 3) is circular with a concentric circular hollow in one face, a groove along the diameter of the other face, and a center hole through the thickness. Along the diameter perpendicular to the groove, three pairs of small eccentric holes are placed at three radial distances. The two outer pairs of holes are threaded. Four additional threaded holes are placed at the same radial distance as the innermost pair of holes at 90° intervals starting 45° from the diameter that passes through the center groove.

7.2.2 *Insert*—The fixture insert is circular with a center hole through the thickness (SI units, see Fig. 4; inch-pound units, see Fig. 5). Two sets of holes are placed along a concentric centerline. These holes align with the innermost set of holes in the outer shell. The set of 4 holes at 90° intervals are counterbored. The insert is fastened inside the hollow of the outer shell to form the concentric groove used to put the specimen in the fixture.

7.2.3 *Adaptor*—The adaptor is circular with a square central torque nut raising out of one face, a flange along a diameter on the other face, and a central hole (SI units, see Fig. 6; inch-pound units, see Fig. 7). Two bolt holes are placed equidistant from the adaptor center on a diameter perpendicular to the centerline of the flange. The adaptor is fastened to the outer shell. The flange of the adaptor fits into the groove of the outer shell. The complete inplane shear specimen/fixture assembly is seen in Fig. 1.

NOTE 1—The outer shell and insert for the compression fixture are the same outer shell and insert used for the fixtures in Test Methods

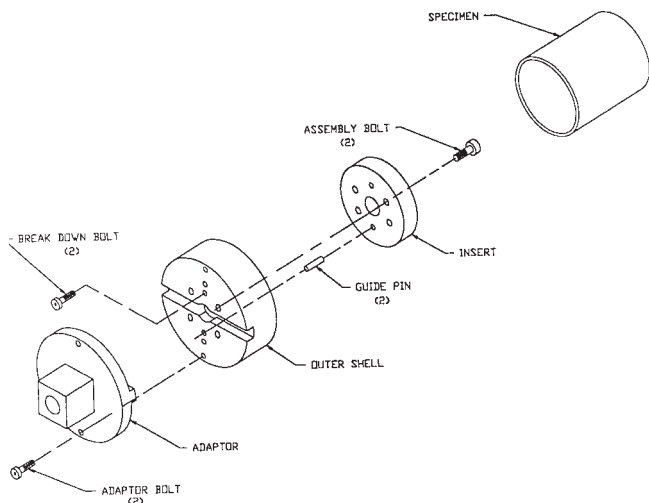


FIG. 1 Assembly Drawing for the Shear Fixture and Specimen

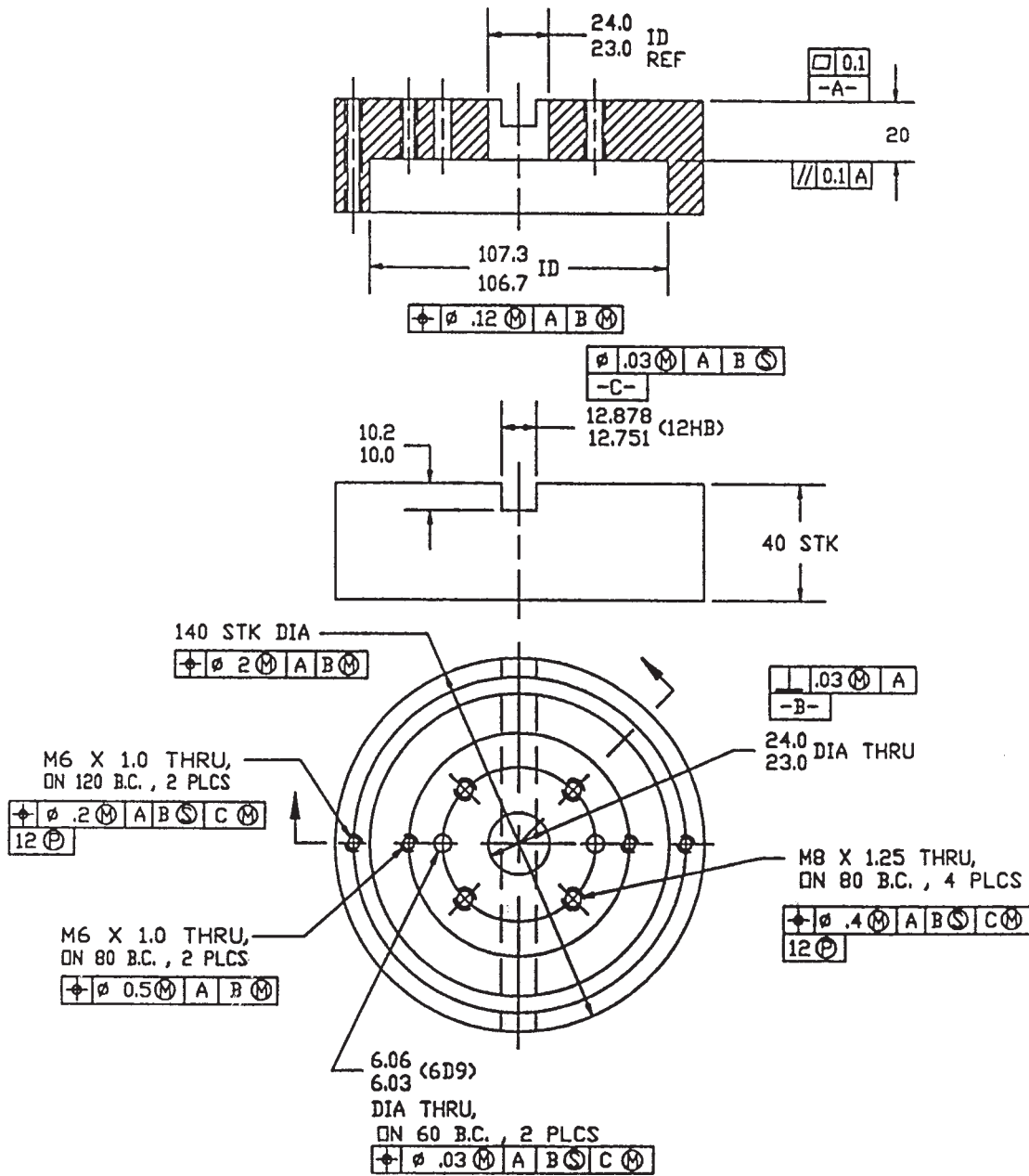


FIG. 2 Outer Shell of the Shear Fixture in SI Units

D 5449/D 5449M and D 5450/D 5450M.

7.3 Testing Machine, comprised of the following:

7.3.1 Fixed Member—A fixed or essentially stationary member, with respect to rotation, to which one end of the torsion specimen/fixture/adaptor assembly, shown in Fig. 3, can be attached.

7.3.2 Rotational Member—A rotational member to which the opposite end of the torsion specimen/fixture/adaptor assembly, shown in Fig. 1, can be attached. Either the rotational member or the fixed member shall be free to move axially to prevent the application of axial forces or the axial load shall be limited to 5 % of the axial strength of the material.

7.3.3 Drive Mechanism, for imparting to the movable member a uniform controlled angular velocity with respect to the

fixed member. This angular velocity is to be regulated as specified in Section 9.

7.3.4 Load Indicator—A suitable load-indicating mechanism capable of showing the total torsional load carried by the test specimen. This mechanism shall be essentially free of inertia-lag at the specified rate of testing and shall indicate the load within an accuracy of $\pm 1 \%$ of the actual value, or better.

7.3.5 Construction Materials—The fixed member, movable member, drive mechanism, fixtures, and adaptors shall be constructed of such materials and in such proportions that the total rotational deformation of the system contributed by these parts is minimized.

7.4 Strain-Indicating Device—Load versus strain data shall be determined by means of bonded resistance strain gages.

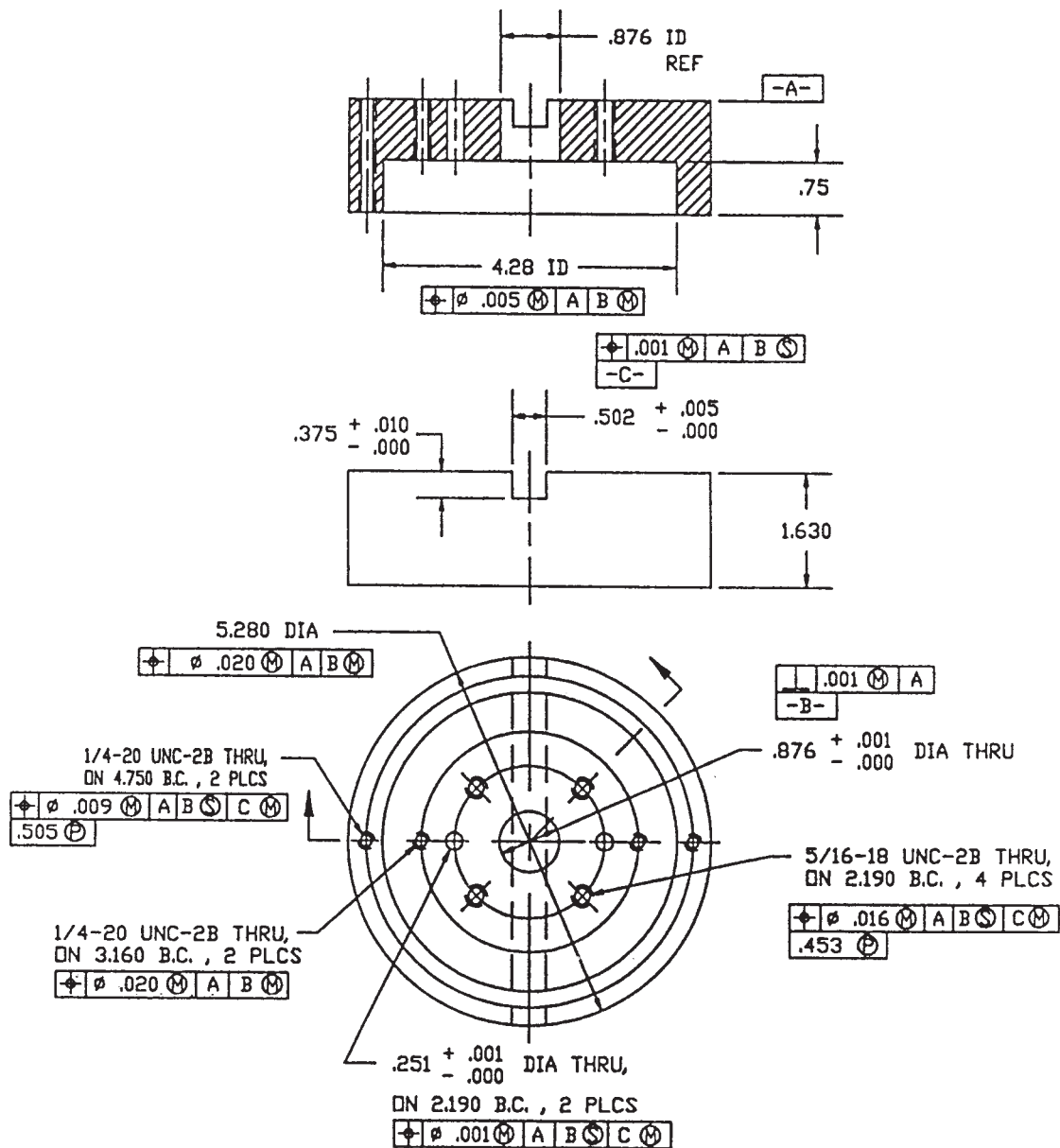


FIG. 3 Outer Shell for the Shear Fixture in Inch-Pound Units

Each strain gage shall be 6.3 mm [0.25 in.] in length. Strain gage rosettes (0°/45°/90°) shall be used to correct for gage misalignment. Gage calibration certification shall comply with Test Method E 251. Some guidelines on the use of strain gages on composites are presented in 7.4.1-7.4.4. A general reference on the subject is Tuttle and Brinson.⁸

7.4.1 *Surface Preparation*—The surface preparation of fiber-reinforced composites discussed in Guide E 1237 can penetrate the matrix material and cause damage to the reinforcing fibers, resulting in improper coupon failures. Reinforcing fibers should not be exposed or damaged during the surface preparation process. The strain gage manufacturer should be

consulted regarding surface preparation guidelines and recommended bonding agents for composites, pending the development of a set of standard practices for strain gage installation surface preparation of fiber-reinforced composite materials.

7.4.2 *Gage Resistance*—Consideration should be given to the selection of gages having larger resistance to reduce heating effects on low-conductivity materials. Resistances of 350Ω or higher are preferred. Additional considerations should be given to the use of the minimum possible gage excitation voltage consistent with the desired accuracy (1 to 2 V is recommended) to further reduce the power consumed by the gage. Heating of the coupon by the gage may affect the performance of the material directly, or it may affect the indicated strain due to a difference between the gage temperature compensation factor and the coefficient of thermal expansion of the coupon material.

⁸ Tuttle, M. E. and Brinson, H. F., "Resistance-Foil Strain-Gage Technology as Applied to Composite Materials," *Experimental Mechanics*, Vol 24, No. 1, March 1984, pp. 54-64; errata noted in Vol 26, No. 2, January 1986, pp. 153-154.

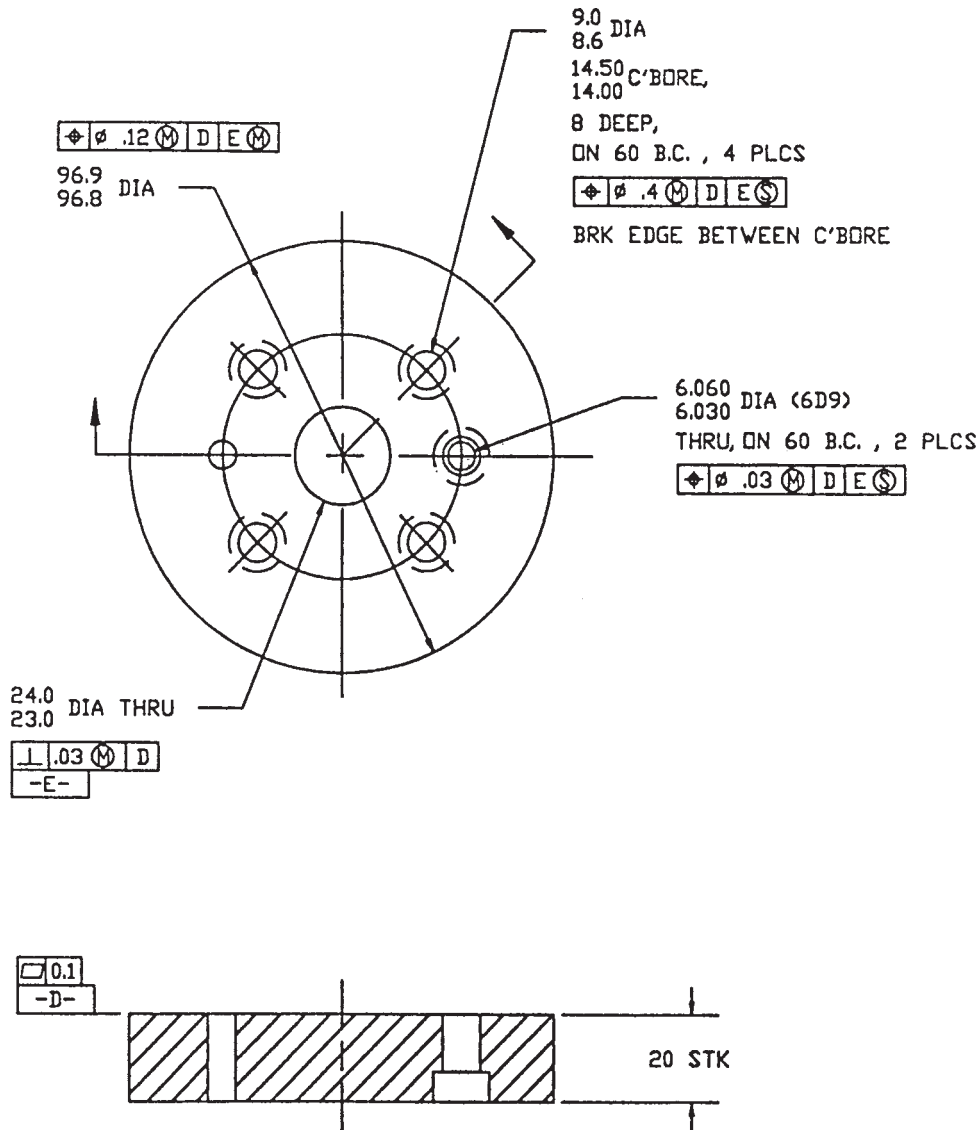


FIG. 4 Insert of the Shear Fixture in SI Units

7.4.3 *Temperature Considerations*—Consideration of some form of temperature compensation is recommended, even when testing at standard laboratory atmosphere. Temperature compensation is required when testing in nonambient temperature environments.

7.4.4 *Transverse Sensitivity*—Consideration should be given to the transverse sensitivity of the selected strain gage. The strain gage manufacturer should be consulted for recommendations on transverse sensitivity corrections and effects on composites.

7.5 *Conditioning Chamber*—When conditioning materials at nonlaboratory environments, a temperature/vapor-level controlled environment conditioning chamber is required which shall be capable of maintaining the required temperature to within $\pm 3^\circ\text{C}$ [$\pm 5^\circ\text{F}$] and the required relative vapor level to within $\pm 3\%$. Chamber conditions shall be monitored either on an automated continuous basis or on a manual basis at regular intervals.

7.6 *Environmental Test Chamber*—An environmental test chamber is required for testing environments other than ambi-

ent testing laboratory conditions. This chamber shall be capable of maintaining the gage section of the test specimen at the required test environment during the mechanical test.

8. Sampling and Test Specimens

8.1 *Sampling*—At least five specimens per test condition should be tested unless valid results can be gained through the use of fewer specimens, such as in the case of a designed experiment. For statistically significant data, the procedures outlined in Practice E 122 should be consulted. The method of sampling shall be reported.

8.2 *Geometry*—The test specimen shall be as shown in Fig. 8. The length of all specimens shall be 140 mm [5.5 in.]. This will provide a 102 mm [4.0 in.] gage length. The inner diameter of all specimens shall be 100 ± 4 mm [4.000 ± 0.015 in.]. Specimens may be fabricated on a tapered mandrel yielding a maximum taper over the specimen length of 0.0005 mm/mm on the diameter. The specimens shall have a nominal wall thickness of 2 mm [0.08 in.], the actual thickness to be

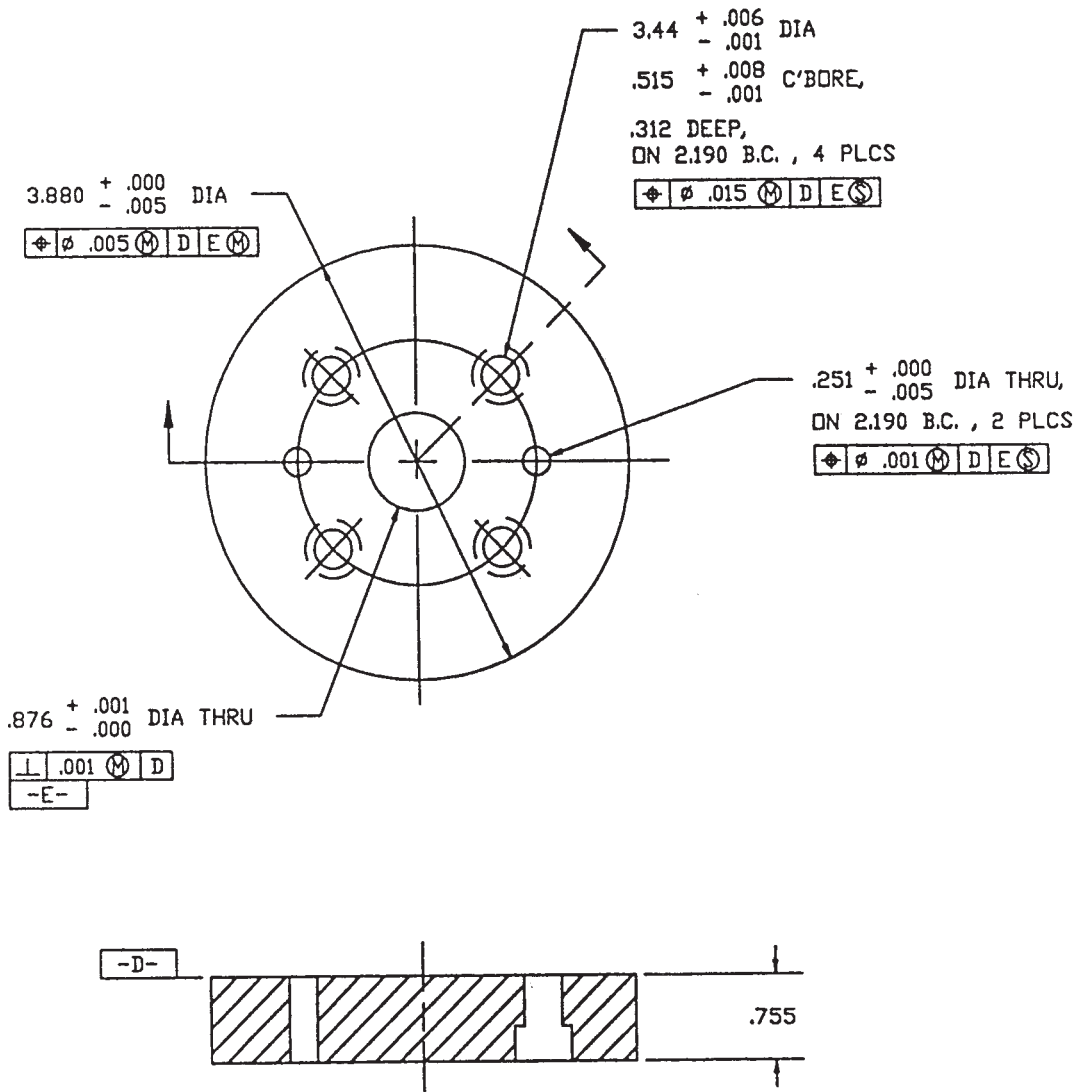


FIG. 5 Insert for the Shear Fixture in Inch-Pound Units

specified by the winding parameters and shall be maintained as the test specimen is wound and cured.

8.3 *Winding*—All specimens shall be hoop wound (approximately 90°) with a single tow and with enough layers to meet the thickness criterion described in 8.2.

9. Calibration

9.1 The accuracy of all measurement equipment shall have certified calibrations that are current at the time of use of the equipment.

10. Conditioning

10.1 *Standard Conditioning Procedure*— Unless a different environment is specified as part of the experiment, the test specimens shall be conditioned in accordance with Procedure C of Test Method D 5229 and stored and tested at standard laboratory atmosphere ($23 \pm 2^\circ\text{C}$ [$73.4 \pm 3.6^\circ\text{F}$] and at $50 \pm 10\%$ relative humidity).

11. Procedure

11.1 *Parameters to be Specified Prior to Test:*

11.1.1 The sampling method, specimen geometry, and test parameters used to determine density and reinforcement volume.

11.1.2 The inplane shear specimen sampling method.

11.1.3 The environmental conditioning test parameters.

11.1.4 The inplane shear property and data reporting format desired.

NOTE 2—Specific material property, accuracy, and data reporting requirements should be determined prior to test for proper selection of instrumentation and data recording equipment. Estimates of operating stress and strain levels should also be made to aid in transducer selection, calibration of equipment, and determination of equipment settings.

11.2 General Instructions:

11.2.1 Any deviation from this test method shall be reported.

11.2.2 Unless otherwise directed, determine specific gravity and reinforcement and void volume percentages for each winding. The material used for the determination of these properties should be extracted from the center of the winding if multiple specimens are extracted from one winding or from

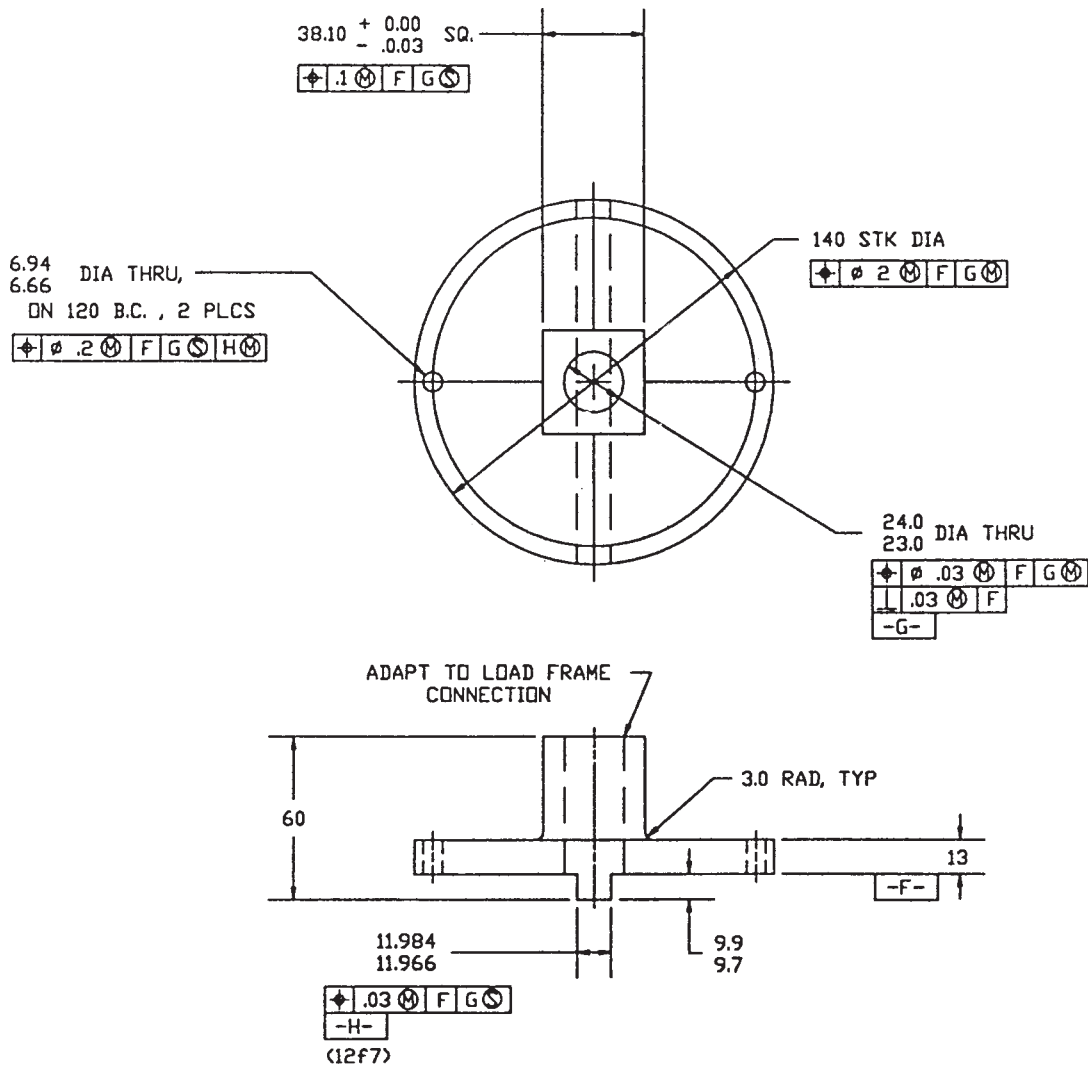


FIG. 6 Adaptor for the Shear Fixture in SI Units

one of the ends of the winding if only one specimen is extracted from the winding. Determine and report specific gravity and density in accordance with Test Methods D 792. Determine and report volume percent of the constituents by one of the matrix digestion procedures of Test Method D 3171, or, for certain reinforcement materials such as glass and ceramics, by the matrix burn-off technique of Test Method D 2584. The void content equations of Test Methods D 2734 are applicable to both Test Method D 2584 and the matrix digestion procedures.

11.2.3 Following any conditioning, but before the testing, measure and report the specimens outer diameter (OD), inner diameter (ID), and length. The specimens are measured by first marking two randomly selected locations within the middle two-thirds of the specimen's length. At each of the points, average four measurements of the outer diameter on an axis that passes through the point and then repeat the procedure on an axis perpendicular to the initial axis. Repeat the procedure for the inner diameter using the same axes. Subtract the average inner diameter from the average outer diameter and divide the remainder by 2. This value will be used as the

composite wall thickness, t_c . Also, obtain 4 length measurements, made at 90° intervals around the specimen circumference, and compute their average. This value will be used as the specimen length.

11.3 *Strain Gage Installation*—Attach strain gages to the center of the specimens gage section. Two strain gage rosettes (oriented as $-45^\circ/0^\circ/45^\circ$, where 0° is parallel to the specimen axis), mounted 180° around the specimen outer circumference from each other as shown in Fig. 8, are recommended in order to ascertain that only torsional loading is being applied. Nontorsional loading may be detected if one strain measured on one rosette is greatly different from the strain on the other rosette.

11.4 *Fixture Assembly*—Assembly of the inplane shear fixture is illustrated in Fig. 1. Place two guide pins into the guide pin holes of the insert such that approximately half of the pins length are protruding from the insert. Place the insert inside the concentric hollow of the outer shell such that the protruding guide pins enter the outer shell guide pin holes. Secure the insert to the outer shell using four assembly bolts. Prior to testing, place adaptor on outer shell such that the outer

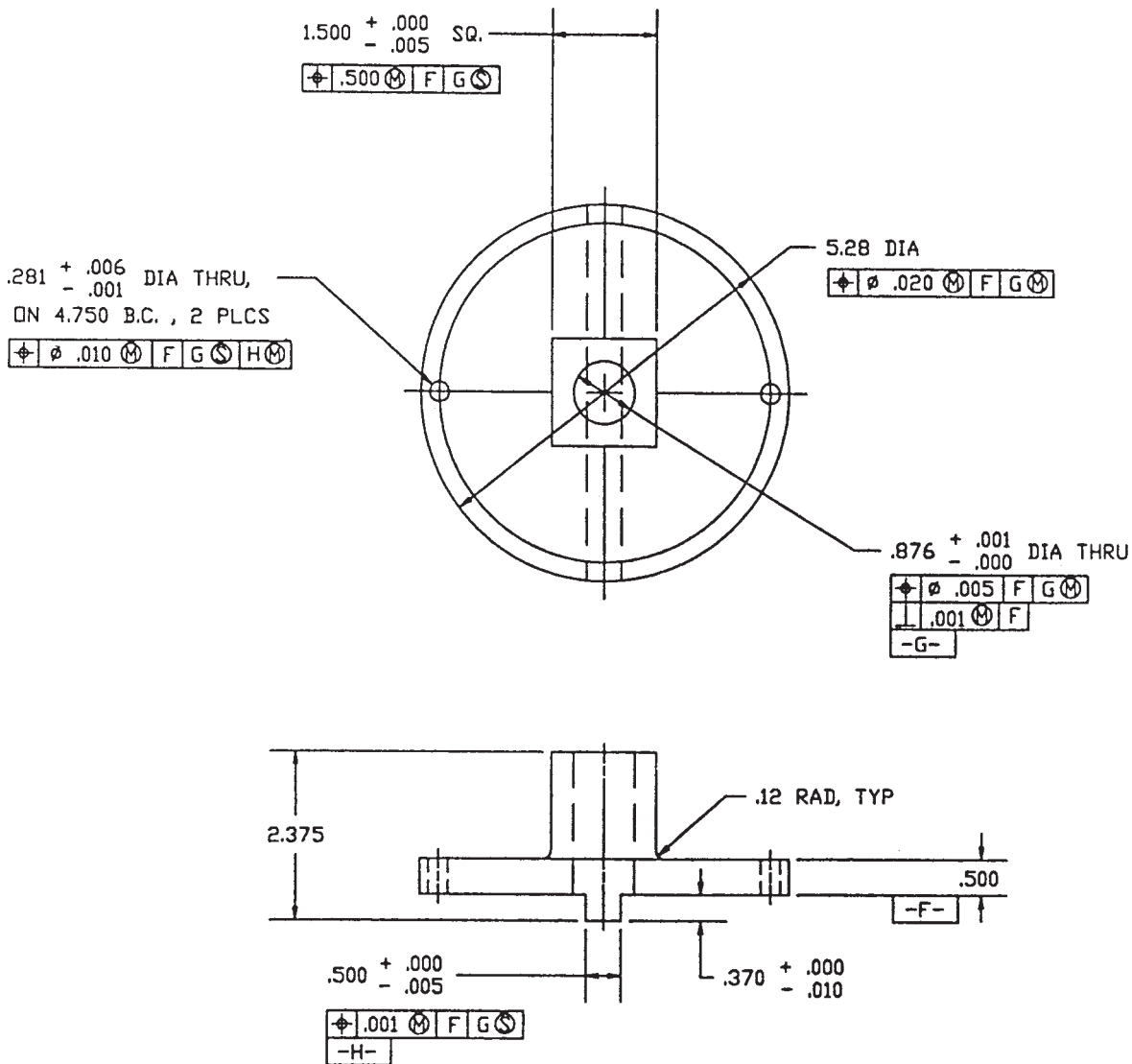


FIG. 7 Adaptor for the Shear Fixture in Inch-Pound Units

shell flange is inserted into the outer shell groove. Secure the adaptor to the outer shell using two adaptor bolts.

11.5 *Securing Specimen*—Secure the test specimen within two fixtures, as shown in Fig. 9, by filling the fixtures cavities with potting material and inserting the specimen ends firmly to the bottom of the cavities while allowing the potting material to form a bead (see Note 3). Cure according to the manufacturer's specifications, but the cure temperature should not jeopardize the specimen. Obtain four measurements of the free length between the fixtures, made at 90° intervals around the specimen/fixture circumference, and compute their average. This value will be used as the gage length.

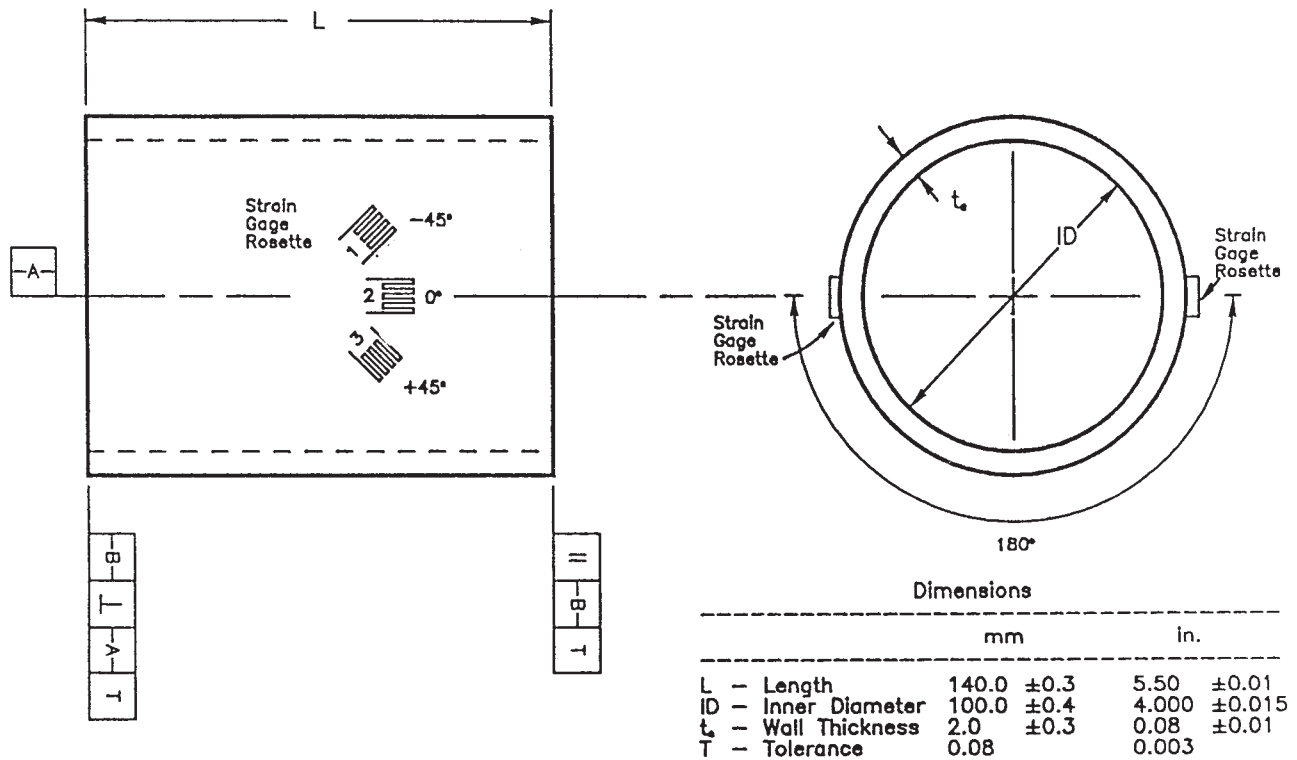
NOTE 3—The potting material should be selected so that it can be cured at a temperature, T_c , no greater than 28°C [50°F] lower than the glass transition temperature T_g of the specimen, $T_c < T_g - 28^\circ\text{C}$ [$T_c < T_g - 50^\circ\text{F}$]. It is helpful if the potting material can be removed without a great deal of difficulty upon completion of the test. A potting material should be selected to have properties sufficient to avoid failure of the potting material and failure of the specimen near the potting material during the test.

11.6 *Speed of Testing*—Speed of testing should be set to effect a nearly constant strain rate in the gage section. If strain control is not available on the testing machine, this may be approximated by repeated monitoring and adjusting of the rate of torque application to maintain a nearly constant strain rate, as measured by strain transducer response versus time. The strain rate should be selected so as to produce failure within 1 to 10 min. If the ultimate strain of the material cannot be reasonably estimated, initial trials should be conducted using standard speeds until the ultimate strain of the material and the compliance of the system are known, and the strain rate can be adjusted. The suggested standard speeds are as follows:

11.6.1 *Constant Torque Speed Machine*—A standard torque speed of 2°/min.

NOTE 4—Use of a fixed torque speed in testing machine systems with a high compliance will result in a strain rate that is much lower than required.

11.7 *Test Environment*—The specimen shall be conditioned to the desired moisture profile and tested under the same



- Notes:
1. Tube may be fabricated on a tapered mandrel with maximum taper of 0.0005 in/in (0.0005 mm/mm) on the diameter.
 2. Actual measure of inner diameter will depend on specimen placement along tapered mandrel during fabrication.

FIG. 8 Test Specimen Shown With Strain Gage Configuration

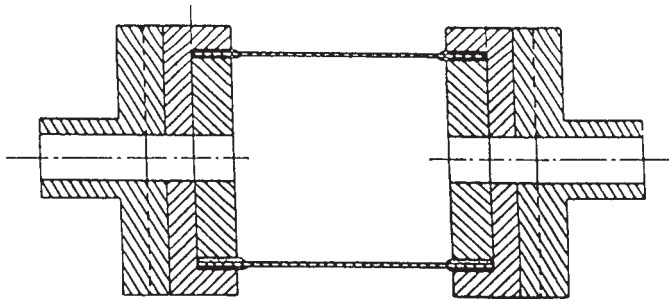


FIG. 9 Specimen/Fixture Assembly

conditioning fluid exposure level. However, cases such as elevated temperature testing of a moist specimen place unrealistic requirements on the capabilities of common testing machine environmental chambers. In such cases, the mechanical test environment may need to be modified, for example, by testing at elevated temperature with no fluid exposure control, but with a specified limit on time to failure from withdrawal from the conditioning chamber. Modifications to the test environment shall be recorded.

11.7.1 If the testing area environment is different than the specimen conditioning environment, then the specimens shall be stored in the conditioned environment until test time.

11.8 *Data Recording Instrumentation*— Attach the data recording instrumentation to the strain gages on the specimen and to the load cell.

11.9 *Loading*—Apply the load to the specimen at the specified rate until failure, while recording data.

11.10 *Data Recording*—Record load versus strain continuously, or at frequent regular intervals. If the specimen is to be failed, record the maximum load, the failure load, and the strain at or as near as possible to where the load drops off significantly. A 10 % load drop off is typically considered significant.

11.11 *Failure Mode*—Record the mode and location of failure of the specimen. Choose, if possible, a standard description from the sketches of common test failure modes as shown in Fig. 10. Failure in a specimen occurring within one specimen thickness of the bond between the specimen and the test fixture is considered a grip (GR) failure. Grip failure is typically precipitated by an anomalous condition; therefore, the grip failure mode is considered inappropriate.

11.12 *Specimen/Fixture Bond*—A significant fraction of failures in a sample population occurring within one specimen thickness of the bond between the specimen and test fixture shall be cause for reexamining the means of load introduction into the material. Factors considered should include alignment of the specimen in the fixture, alignment of the fixtures in the grips, and material used to bond the specimen to the fixture.

11.13 *Fixture Disassembly*—This is only an advised procedure for disassembling the test fixture. Remove the two adaptor bolts from the adaptor and detach adaptor from outer shell. Cut

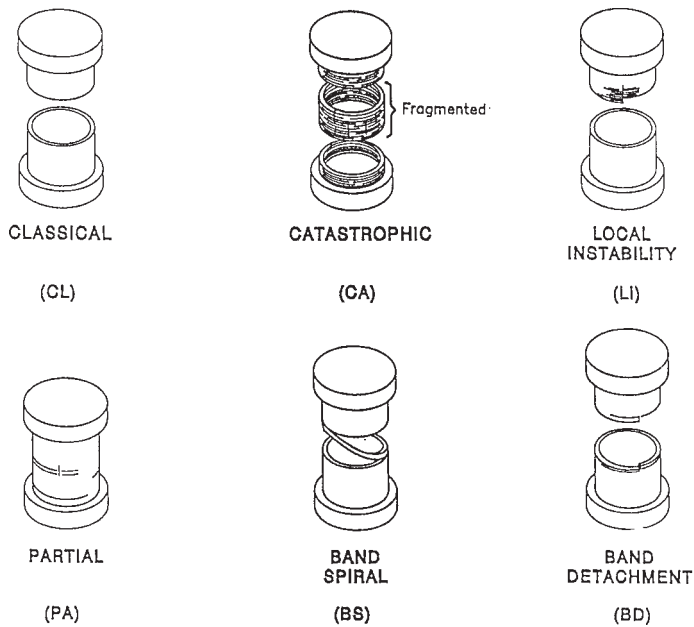


FIG. 10 Failure Modes for Hoop Wound Tubes in Inplane Shear

each end of the specimen at the base of the fixture. Remove the four assembly bolts from the insert. Place the outer shell and insert assembly into an oven at a temperature that will degrade the potting compound. After a sufficient period of time, remove the fixtures from the oven and allow them to cool. Insert two break down bolts into the outer shell (see Fig. 1). Turn the break down bolts to force the insert out of the concentric hollow of the outer shell. Remove the guide pins from the insert and the outer shell. Wire brush the insert and the outer shell to remove specimen debris.

12. Calculation

12.1 *Transverse Sensitivity Correction*—Correct the strain gage readings for transverse sensitivity separately for each rosette as follows:

$$\epsilon_1^i = \frac{\epsilon_1^i (1 - \nu_o K_{t1}) - K_{t1} \epsilon_3^i (1 - \nu_o K_{t3})}{1 - K_{t1} K_{t3}} \quad (1)$$

$$\epsilon_2^i = \frac{\epsilon_2^i (1 - \nu_o K_{t2})}{1 - K_{t2}}$$

$$\frac{-K_{t2} [\epsilon_1^i (1 - \nu_o K_{t1}) (1 - K_{t3}) + \epsilon_3^i (1 - \nu_o K_{t3}) (1 - K_{t1})]}{(1 - K_{t1} K_{t3}) (1 - K_{t2})}$$

$$\epsilon_3^i = \frac{\epsilon_3^i (1 - \nu_o K_{t3}) - K_{t3} \epsilon_1^i (1 - \nu_o K_{t1})}{1 - K_{t1} K_{t3}}$$

where:

ν_o = Poisson's ratio for the material used in calibration by the strain gage manufacturer (usually 0.285),

K_{t1}, K_{t2}, K_{t3} = transverse sensitivity coefficients for gages 1, 2, and 3, respectively (these values are typically reported by the manufacturers in percentages and must be converted for use in the above equations, for example, $K_t = 0.7\% = 0.007$),
 $\epsilon_1^i, \epsilon_2^i, \epsilon_3^i$ = the indicated (uncorrected) strains from gages 1, 2, and 3, respectively, for the i^{th} rosette, and
 $\epsilon_1^i, \epsilon_2^i, \epsilon_3^i$ = the corrected strains for gages 1, 2, and 3, respectively, for the i^{th} rosette.

12.2 *Maximum Shear Strain Calculation*—Calculate separately for each rosette the maximum shear strain in the material that results from the applied load and the angle from the principal directions using the corrected strain gage readings as follows:

$$\gamma_{12}^i = \epsilon_1^i - \epsilon_3^i)^2 + (2\epsilon_2^i - \epsilon_1^i - \epsilon_3^i)^2]^{1/2} \quad (2)$$

where γ_{12}^i = maximum shear strain for the i^{th} rosette. If γ_{12}^i varies by more than 5% with location of rosette around the cylinder, within the strain range used to calculate the shear modulus (see 12.6), the strain field is not uniform and the test is invalid.

12.3 *Calculation of Angle of Rotation from Principal Plane*—Calculate separately for each rosette the angle of rotation of the rosette from the principal plane using the corrected strain gage readings as follows:

$$\theta^i = \frac{1}{2} \tan^{-1} \frac{2\epsilon_2 - \epsilon_1 - \epsilon_3}{\epsilon_3 - \epsilon_1} \quad (3)$$

where θ^i = the angle of rotation of the i^{th} rosette from the principal plane.

If θ^i for any of the rosettes around the cylinder is greater than $\pm 10^\circ$, the calculation of the maximum shear strain is not considered reliable and the test is invalid.

NOTE 5—(Eq 2) and (Eq 3), used to calculate the maximum shear strains and the angle of rotation from the principal plane, were developed specifically for gages configured as illustrated in Fig. 8.

12.4 *Average Maximum Shear Strain*—Calculate the average maximum shear strain in the material as follows:

$$\bar{\gamma}_{12} = \sum_{i=1}^n \gamma_{12}^i / n \quad (4)$$

where:

$\bar{\gamma}_{12}$ = average γ_{12} for the rosettes, and

n = number of rosettes on the test specimen (usually two).

Record the average maximum shear strain at failure, $\bar{\gamma}^u_{12}$.

12.5 *Inplane Shear Strength*—Calculate the shear stress at failure, τ^u_{12} , using the following:

$$\tau_{12}^u = \frac{16T_{\max} \text{OD}}{\pi(\text{OD}^4 - \text{ID}^4)} = \frac{T_{\max} r_{\max}}{J} \quad (5)$$

where:

T_{\max} = the maximum torque applied to the cylinder,
 J = the polar moment of inertia,

$$J = \frac{\pi}{32} (\text{OD}^4 - \text{ID}^4) \quad (6)$$

r_{\max} = the maximum radial distance,

$$r_{\max} = \frac{\text{OD}}{2} \quad (7)$$

and ID and OD = the average inner and outer diameters, respectively.

12.6 *Inplane Shear Modulus*—Select the appropriate chord modulus strain range from Table 1. Calculate the inplane shear modulus using the following:

$$G_{12} = \Delta \tau_{12} / \Delta \bar{\gamma}_{12} \quad (8)$$

where:

G_{12} = inplane shear modulus, MPa [psi],
 $\Delta \tau_{12}$ = difference in applied shear stress between the two strain points of Table 1, MPa [psi], and
 $\Delta \bar{\gamma}_{12}$ = difference between the two shear strain points of Table 1 (nominally either 0.001, 0.002, or 0.005).

If data is not available at the exact strain range end points (as often occurs with digital data), use the closest available data points. Report the shear modulus to three significant figures. Also report the strain range used in the calculation.

12.6.1 The tabulated strain ranges should only be used for materials that do not exhibit a transition region (a significant change in the slope of the stress strain curve) within the given strain range. If a transition region occurs within the recommended strain range, then a more suitable strain range shall be used and reported.

12.6.2 *Inplane Shear Modulus (Other Definitions)*—Other definitions of elastic modulus may be evaluated and reported at the user's discretion. If such data is generated and reported, report also the definition used, the strain range used, and the results to three significant figures. Test Method E 111 provides additional guidance in the determination of moduli of elasticity.

12.7 *Statistical Requirements*—For each series of valid tests calculate the average value (\bar{x}), standard deviation (s), and coefficient of variation (cv) for each strength, strain at failure, modulus, and Poisson's ratio as follows:

$$\bar{x} = \sum_{i=1}^n x_i \quad (9)$$

$$s = \left[\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1} \right]^{1/2} \quad (10)$$

$$cv = s / \bar{x} \quad (11)$$

where:

x_i = test value, and
 n = number of samples.

13. Report

13.1 Report the following information:

13.1.1 Complete identification of the material tested, including type, source, manufacturer's code number, form, fiber volume fraction, void content, filament count, ply sequence and wind angle, fiber and resin lot, and any previous history.

13.1.2 Complete description of the method of fabricating the specimens, including processing details.

13.1.3 Density, fiber volume fraction, and void content for each winding.

13.1.4 Complete description of the testing equipment used including the test machine, load cell, strain gages, data acquisition system, and estimates of error for each parameter measured. Identification of potting material, radius of bead, and cure temperature.

13.1.5 Conditioning procedures used if other than specified in test method.

13.1.6 Relative humidity and temperature conditions in the test room.

13.1.7 Test method used, including type and rate of loading.

13.1.8 Number of specimens tested and identification number for each specimen.

13.1.9 *Test Specimen Dimensions*—The outer diameter, inner diameter, wall thickness (t_w), total length, and gage length for each specimen, average values, standard deviations, and coefficient of variation.

13.1.10 Shear strength for each specimen, average value, standard deviation, and coefficient of variation for valid tests.

13.1.11 Shear strain at failure, average value, standard deviations, and coefficient of variation for valid tests.

13.1.12 Shear modulus for each specimen, average value, standard deviation, and coefficient of variation for valid tests. Include how the modulus was determined and at what point or between what points on the load versus strain or stress versus strain curve.

13.1.13 Full load versus strain or stress versus strain curves for the averages of the two rosettes. If average curves cannot be calculated, the individual load versus strain or stress versus strain curves corresponding to each strain gage should be reported.

13.1.14 Mode of failure and failure location in specimen. Use Fig. 10 to describe the gage section failure modes. Multiple failure modes can occur in a specimen. Any failure that involves the portion of the specimen bonded to the grips is considered a grip failure (GR).

TABLE 1 Specimen Shear Modulus Calculation Strain Ranges

Maximum Shear Strain Capability of Material, $\mu\epsilon^A$	Shear Modulus Calculations	
	Shear Strain Range	
	Start Point, $\mu\epsilon$	End Point, $\mu\epsilon$
<6000	500	1500
≥ 6000 but <12 000	1000	3000
$\geq 12 000$	1000	6000

^A 1000 $\mu\epsilon$ = 0.001 absolute strain.

13.1.15 Date of test.

13.1.16 Quality assessment of the test data (for example, acceptable, questionable, invalid, etc.), deviations from this test method, and an explanation.

14. Precision and Bias

14.1 *Interlaboratory Test Program*—An interlaboratory study was run in which randomly drawn test specimens of one material (graphite/epoxy) were tested for shear strength, modulus, and strain to failure in each of 6 laboratories (5 laboratories where noted), with each laboratory testing 15 specimens of material. Except for the use of only one material and five laboratories where noted, Practice E 691 was followed for the design and analysis of the data.

14.2 *Test Results*—The precision information given in 14.3 in percentage of the average shear strength, modulus, and strain

to failure (*CV* %) is for the comparison of two test results, each of which is the average of five test determinations.

14.3 Precision:

	τ_{12}^u	G_{12}	τ_{12}^u
Repeatability coefficient of variation	8.1 %	5.4 %	15.6 %
Reproducibility coefficient of variation	10.0 %	7.2 %	17.7 %

NOTE 6—The precision estimates for modulus (G_{12}), and strain to failure (γ''_{12}) are based on data from five laboratories.

14.4 *Bias*—Bias cannot be determined for this test method because an acceptable reference standard does not exist.

15. Keywords

15.1 composite materials; filament winding; inplane shear modulus; inplane shear properties; inplane shear strength; tubes

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