

Column Slenderness

A column is short if:

non-sway (braced) frame [10.10.1]

$$\frac{k l_u}{r} \leq 34 - 12 \left(\frac{m_1}{m_2} \right) \leq 40$$

- assume k (unless specified)

$l_u =$ unbraced

radius of gyration

$$r = \sqrt{\frac{I_g}{A_g}} = \sqrt{\frac{\frac{1}{12} b h^3}{bh}} = \sqrt{\frac{1}{12}} h$$

$m_1 \equiv$ minimum moment

$m_2 \equiv$ maximum moment

$\left(\frac{m_1}{m_2} \right) = (+)$ single curvature D

$(-)$ double curvature B

SWAY (unbraced) [10.10.1]

$$\frac{k l_u}{r} \leq 22$$

* The focus in this class is NON-sway Frames with short columns *

Short \equiv Non-Slender

Column Design

- Structural Analysis

- Estimate column cross section [2-4]

- Analyze using interaction diagram [5-7]

- Iterate

- Detail Column [8-12]

* Focus on tied columns *

Columns

Slenderness

Sway

Design

Gross Area

Details

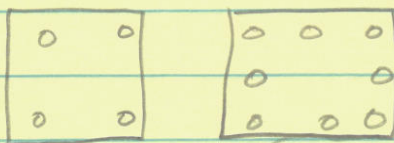
Example

Eccentric loads

Example

- Estimate Gross AREA
 - Assume column is square & has steel on all faces

symmetric



$A_g \xi$

can vary

reinforcement ratio

$$A_g \geq \frac{P_u}{0.45 (f_c' + f_y \rho_{TRIAL})}$$

ρ_g = reinforcement ratio

$$\rho_g = \frac{A_s}{A_g} = \frac{A_s}{bh} \quad 0.01 - 0.03 \text{ typically}$$

$$0.01 \leq \rho_g \leq 0.08 \quad [10.9.1]$$

- Column Details

TIES [7.10.5]

longitudinal bars $\leq \#10, \#3$

" " " " $\#14, \#18, \#4$

Maximum spacing of ties.

min { $16d_p$ of longitud. bars
 $48d_b$ of ties
 min b, h

See [7.10.5.4] if near slab

- Shear [11.2.1.2]
ties act as shear stirrups

- Example Design a rectangular column (tied)
with long side equal to two times the short side.

$$P_D = 650 \text{ k}$$

$$P_L = 400 \text{ k}$$

$$f'_c = 3 \text{ ksi}$$

$$f_y = 60 \text{ ksi}$$

initially assume $e_{\text{gross}} = 0.02$

Select column size

$$A_{\text{steel}} = e A_g$$

$$P_u = 1.2(650 \text{ k}) + 1.6(400 \text{ k}) = 1420 \text{ k}$$

$$\phi P_n = 0.80 \phi [0.85 f'_c (A_g - A_{st}) + f_y A_{st}]$$

$$\rightarrow 1420 = 0.80(0.65)[0.85(3)(A_g - 0.02 A_g) + 60(0.02 A_g)]$$

$$A_g = 738.25 \text{ in}^2$$

↳ use 20x40 column ($A_g = 800 \text{ in}^2$)

Select reinforcement bars

$$1420 = 0.80(0.65)[0.85(3)(800 - A_{st}) + 60(A_{st})]$$

$$A_{st} = 12.02 \text{ in}^2$$

use 8 #11 bars (12.50 in^2)

Design TIES

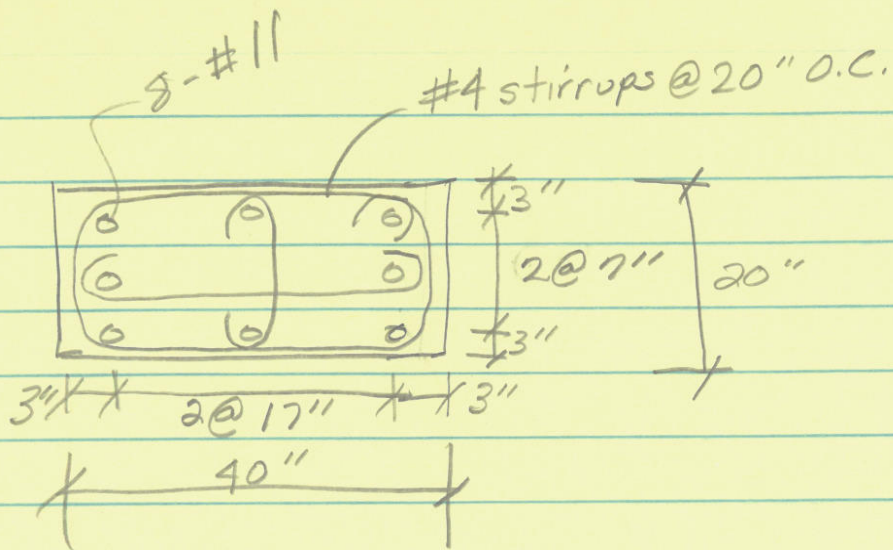
max spacing = min

$$16d_b \leftarrow \begin{matrix} \text{longitudinal} \\ \text{bars} \end{matrix} = 16(1.41) = 22.56 \text{ ''}$$

$$48d_b = 48(0.5) = 24 \text{ ''}$$

least column dim = 20''

use #4 ties
@ 20" o.c.



Check code 7.10.5 for maximum spacing of vertical bars

Design of Eccentrically Loaded Columns Using Interaction Diagrams

11/8/10

If we prepared them for all combinations there would be too many.

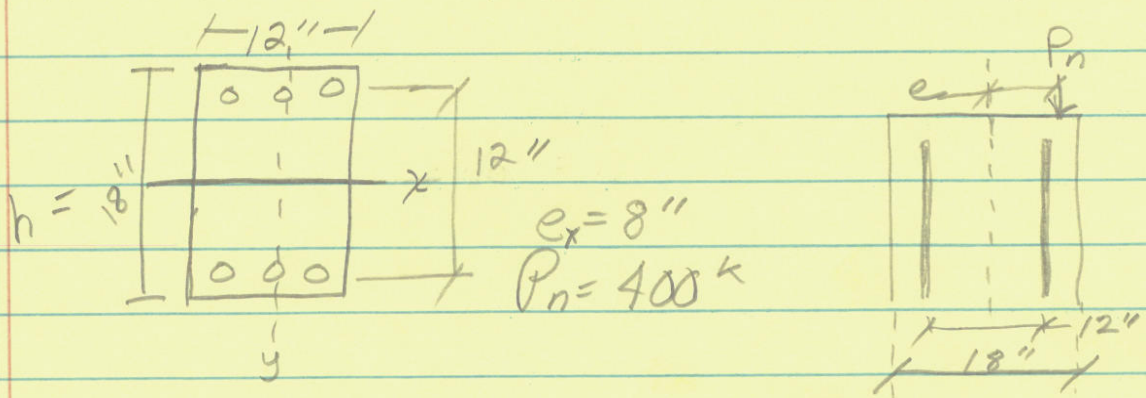
Column Design
Using Interaction
Diagrams
Examples

$$x\text{-axis: } \frac{P_n e}{f'_c A_g h} = R_n$$

$$y\text{-axis: } \frac{P_n}{f'_c A_g} = k_n$$

Warning: Be sure the picture agrees with the column being consider'd

Example: Use the interaction curves in Appendix A to select reinforcing $f'_c = 4 \text{ ksi}$ $f_y = 60 \text{ ksi}$



① Structural Analysis (done already)

$$P_n = 400 \text{ k}$$

$$M_{n_x} = P_n \cdot e_x = (400 \text{ k})(8") = 3200 \text{ in-k}_x$$

② Select column cross section
- already done

③ Analyze Column

$\frac{b}{h}$ about bending axis

Left side of chart

$$\gamma = \text{ratio} = \frac{12''}{18''} = 0.667$$

$$K_n = \frac{P_n}{f'_c A_g} = \frac{400k}{4 \text{ ksi} (12'' \times 18'')} = 0.463$$

Bottom of chart

$$R_n = \frac{P_n e}{f'_c A_g h} = \frac{(400k)(8'')}{(4 \text{ ksi})(12'')(18'')(18'')} = 0.206$$

From chart 0.60

interpolate

From chart 0.70

γ	0.600	0.667	0.70
e_g	0.03	0.026	0.024

$$A_g = \rho_g b h = 0.026 (12)(18)$$

$$A_g = 5.62 \text{ in}^2 \quad \text{use 6 \#9} \quad (A_g = 6.0 \text{ in}^2)$$

Check fit of bars [7.6.3]

Clear Distance $\left(\begin{array}{l} \text{min. } 1.5 d_b \text{ or } 1\frac{1}{2}'' \text{ [7.6.3]} \\ \frac{4}{3} \text{ max agg. size (3,3.2)} \end{array} \right)$

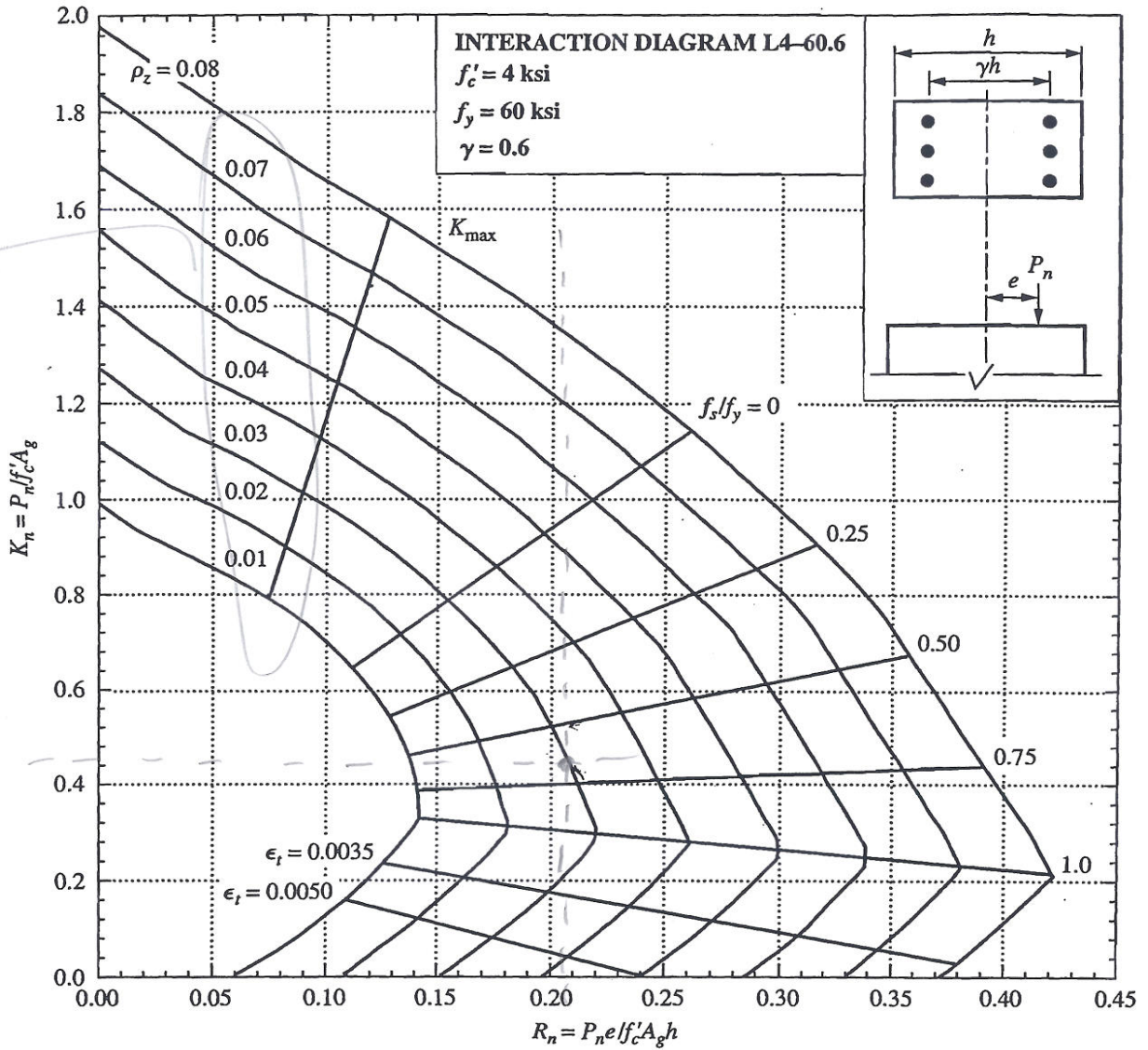
$$1.5(1.25) = 1.6875$$

$$1.5 \longrightarrow 1.5''$$

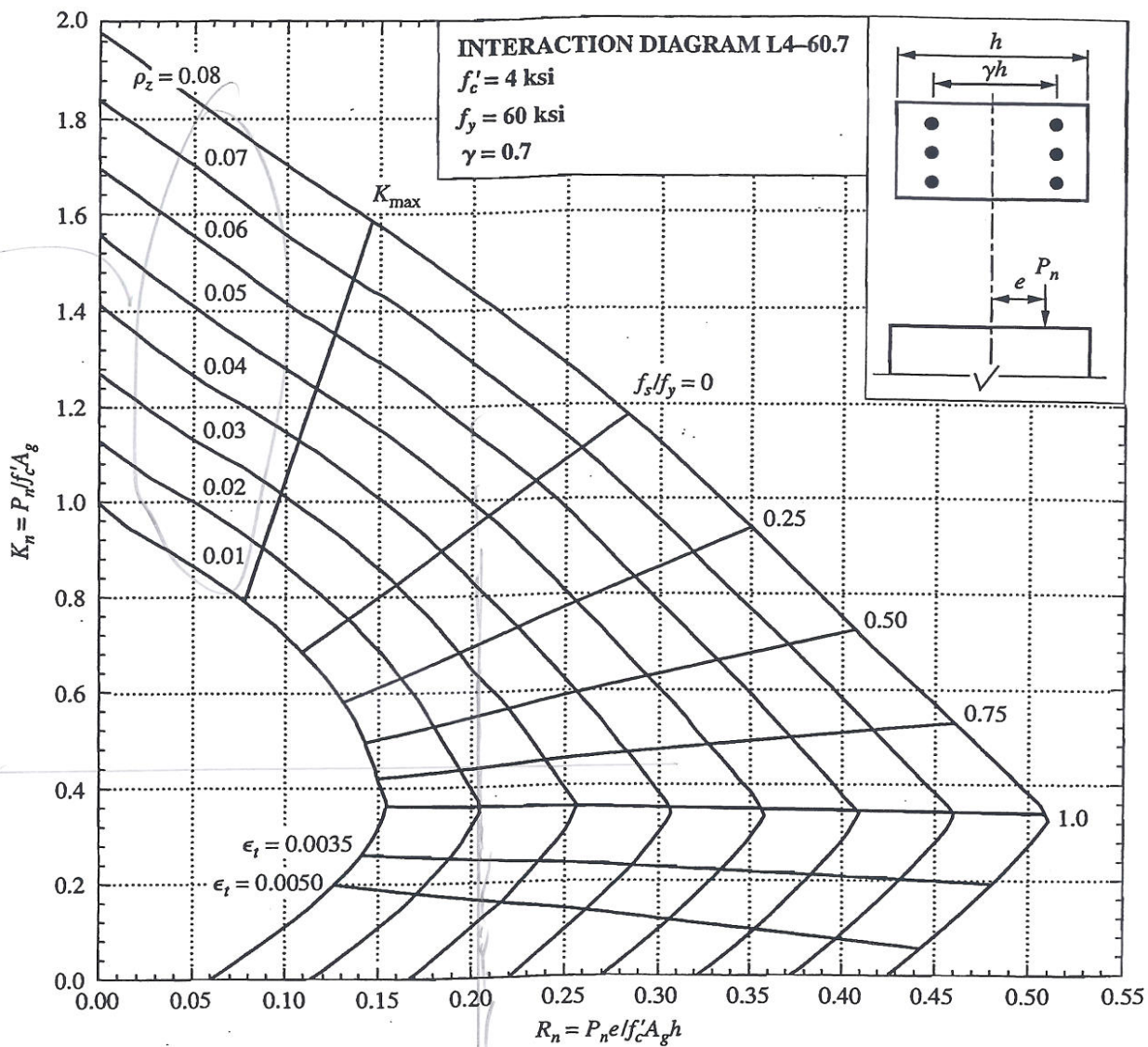
$$\frac{4}{3}(1'') = 1.25$$

$$b_{\text{req}} = \underbrace{3(1.25)}_{\text{bars}} + \underbrace{2(\frac{3}{8})}_{\text{Ties}} + \underbrace{2(1.5)}_{\text{Spacing between bars}} + \underbrace{2(1)}_{\text{cover}}$$

$$= 9.125 < 12'' \quad \text{OK}$$



Graph 2 Column interaction diagrams for rectangular tied columns with bars on end faces only. (Graphs 2 through 13 are published with the permission of the American Concrete Institute.)



Graph 3 Column interaction diagrams for rectangular tied columns with bars on end faces only.

Ties
#3 bars for #9 longitudinal bars

$$Tie S_{max} = \min \begin{cases} 16 d_{bar} = 16(1.125) = 18'' \\ 48 d_{tie} = 48(\frac{3}{8}) = 18'' \\ b = 12'' \end{cases}$$

$$S_{max} = 12''$$

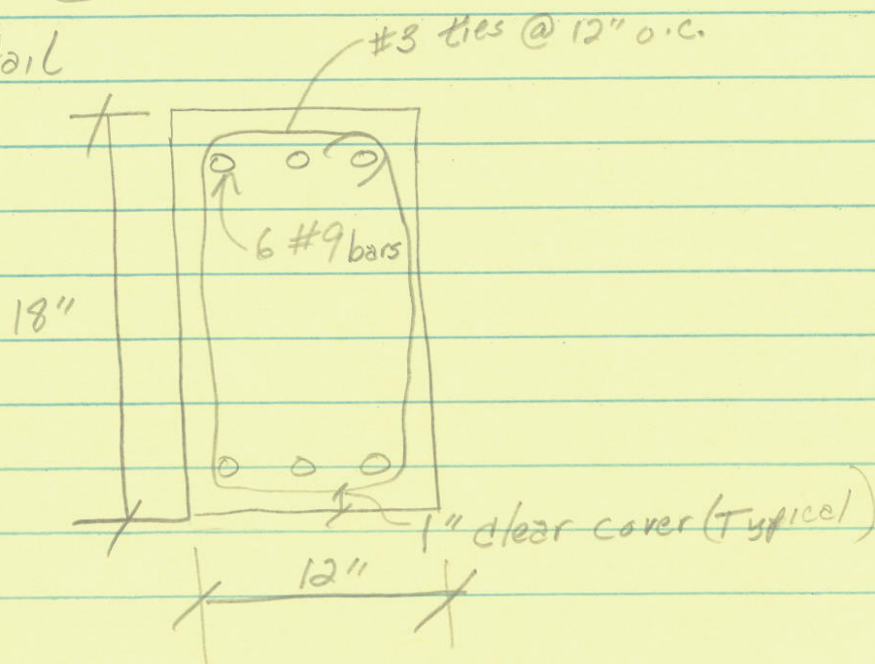
Check Shear

$$V_c = 2 \left[1 + \frac{N_u}{2000 A_g} \right] \sqrt{f'_c} b_w d \quad [eq 11-4]$$

*

* Accounts for increased capacity due to aggregate interlock

#5 Detail

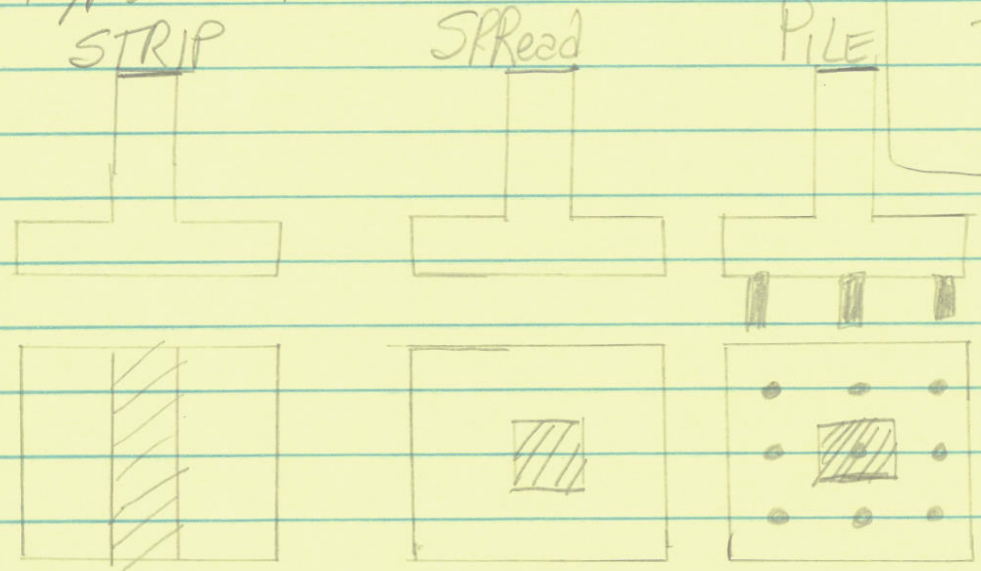


→ Purpose of foundations
 To safely transmit load from the structure to the ground without unsafe differential settlement

Foundations
 Types
 Soil Pressures
 Kern
 Limit States
 A required
 Design of
 Footings
 Soil Failure
 One-Way Slab
 Zway Shear
 Flexure
 Bearing/Load
 Transfer

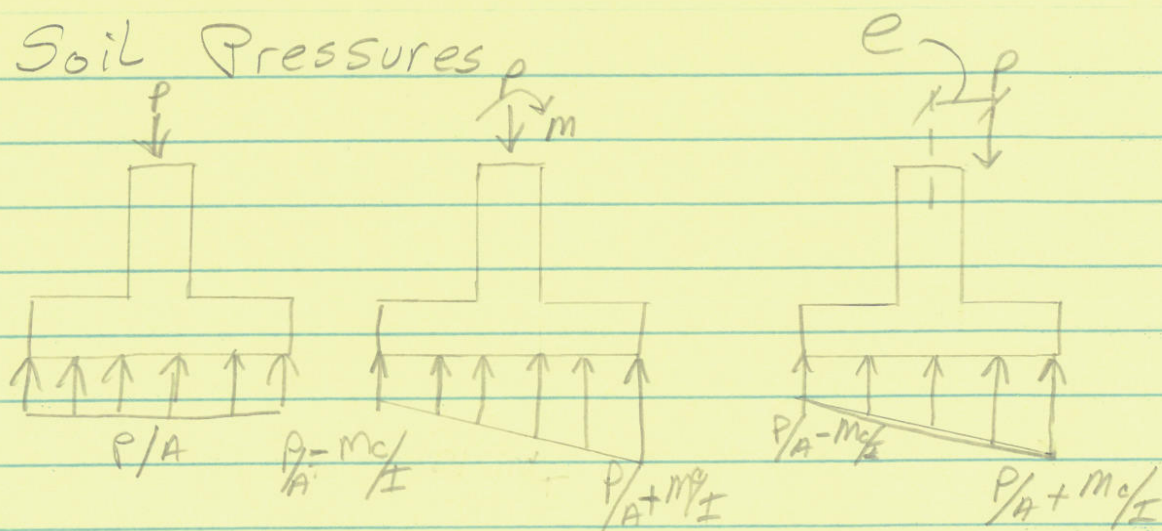
→ What if settlement?
 EVEN → Not huge deal (Mexico City)
 UNEVEN → BIG DEAL (Las Vegas Casino Leaning Tower of Piza)

→ Types of Foundation

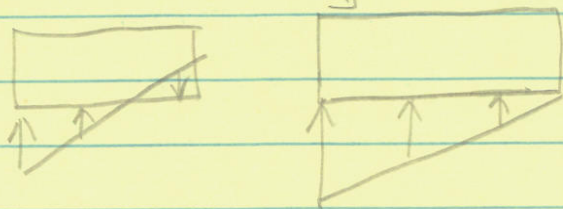
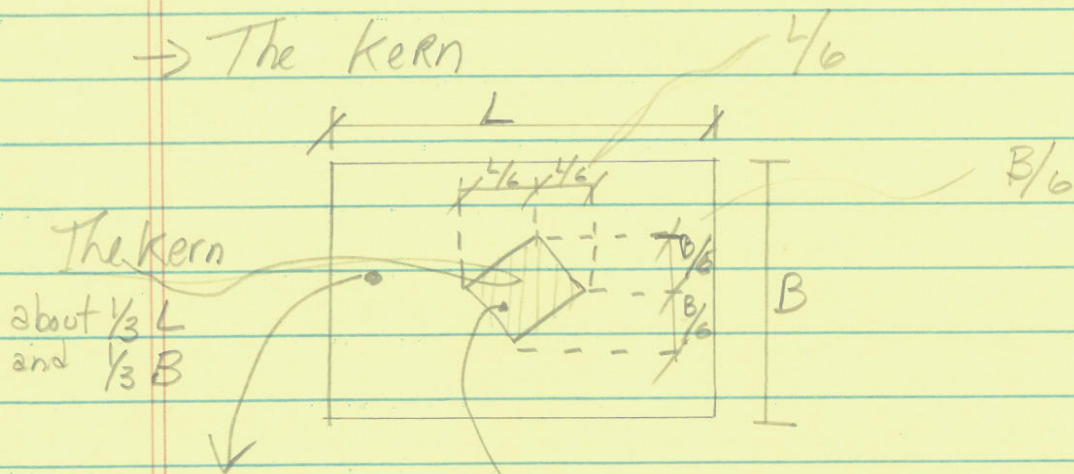


→ Raft or Mat
 Large foundation under entire structure

→ Soil Pressures



→ The Kern



* Load must fall in the kern of the footing

→ Soil Limit

- Soil bearing failure

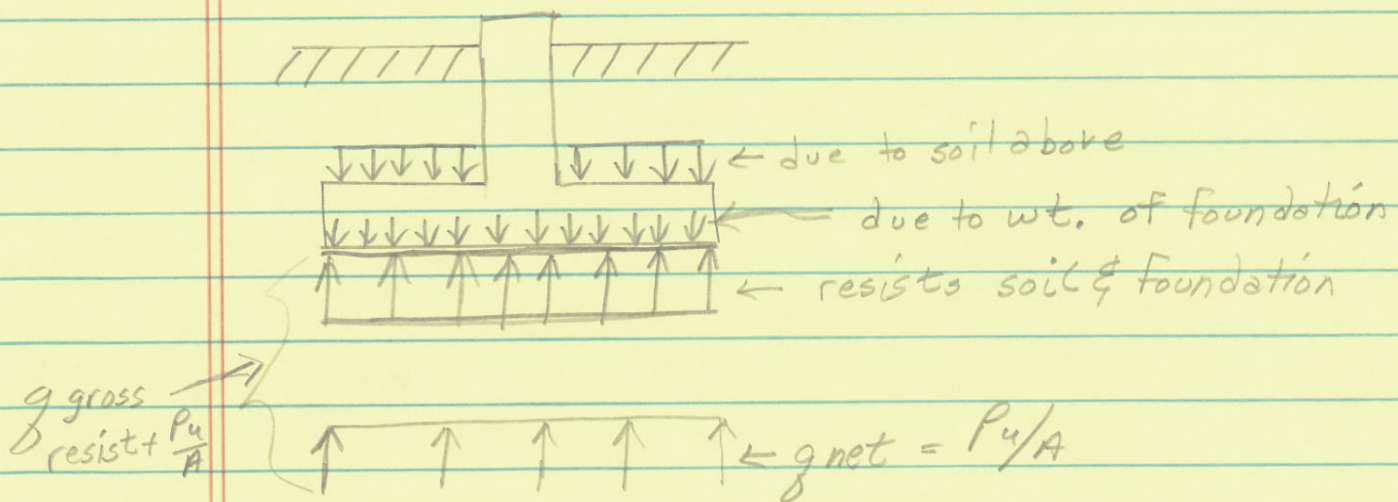
$$g_{act} < g_{allow} = \frac{g_{ultimate}}{FS}$$

g_{act} ↑ From service loads
 $g_{ultimate}$ ← From geo tech
 FS ← usually 2.5 - 3.0

- differential settlement

- excessive settlement

→ Calculations of Soil Pressure



→ A required of Spread Footing

Soil Capacity

$$g_{gross} \leq g_{all}$$

$$A_{req'd} = \frac{D \left\{ \begin{array}{l} \text{structure} \\ \text{footing} \\ \text{over burden} \end{array} \right\} + L}{g_{allowed}}$$

service loads

→ other structural elements

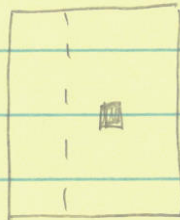
$$q_{net} = \frac{\text{Max factored Load}}{A_{footing}}$$

usually $1.2D_L + 1.6U_L$

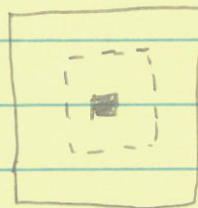
→ Spread footing Limit State (things we need to check)
Soil Failure $q_{act} \leq q_{allowed}$

Shear

1 way →

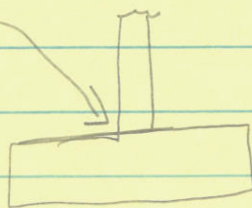


2 way ⇒



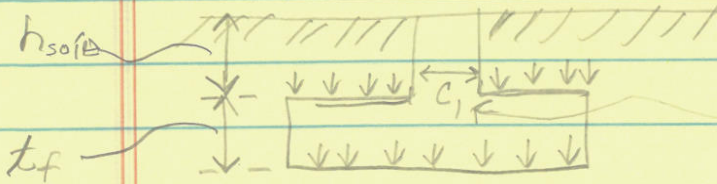
→ Flexure $\phi M_n \geq M_u$
 l_d

→ Bearing / Load transfer
@ joint



Soil Failure

P_D, P_L



h_{soil} = depth of surcharge
 t_f = thickness of footing
 rule of thumb $\approx 1.5c_1$

$q_{actual} \leq q_{allowed}$ ASD

$$q_{act} = \gamma_{soil} h_{soil} + \underbrace{W_{t_f}}_{\text{weight of footing}} + \frac{P_D + P_L}{A_{required}}$$

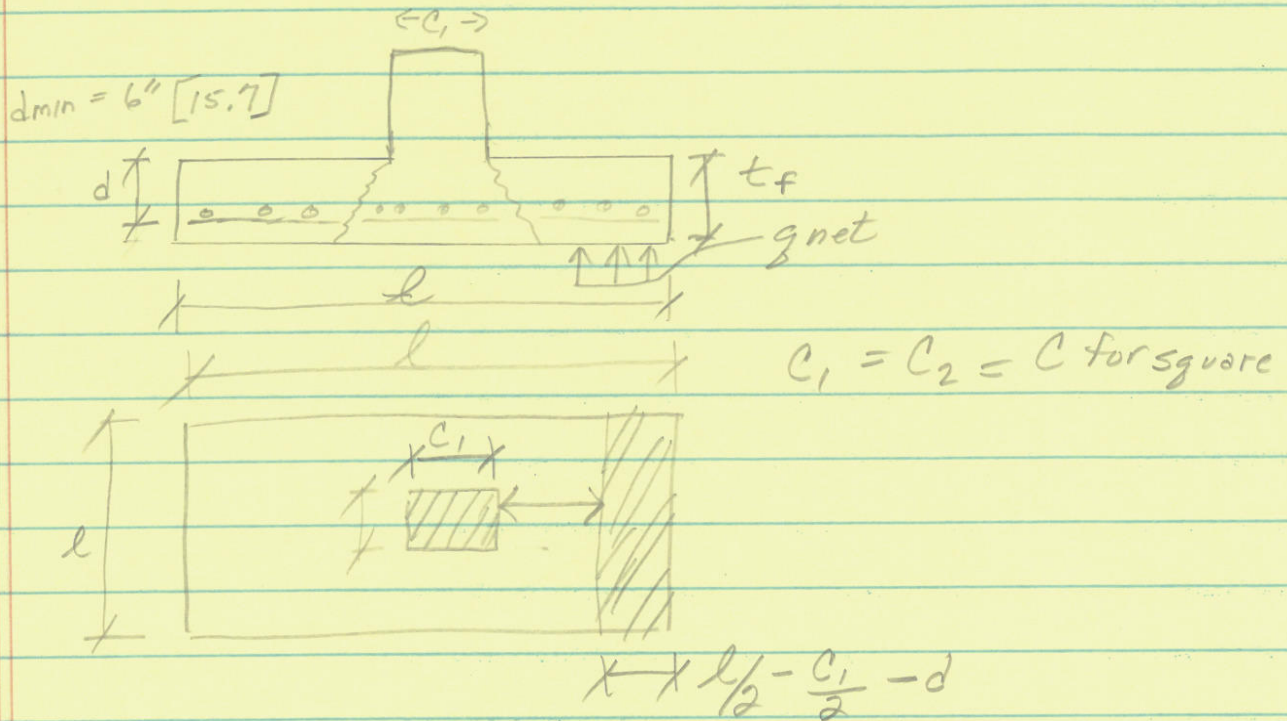
$$\frac{P_D + P_L}{A_{req}} \leq q_{allowed} - \gamma_s h_s - w_{d f}$$



$$A_{req} = \frac{P_D + P_L}{\underbrace{q_{allowed}}_{\text{max allowed}} - \underbrace{\gamma_s h_s}_w - \underbrace{w_{d f}}_w}$$

max allowed - soil - footing

⇒ One Way Shear



$$V_u = l \left(\frac{l}{2} - \frac{c}{2} - d \right) g_{net}$$

$$V_c = 2 \sqrt{f'_c} l d \quad \phi = 0.75$$

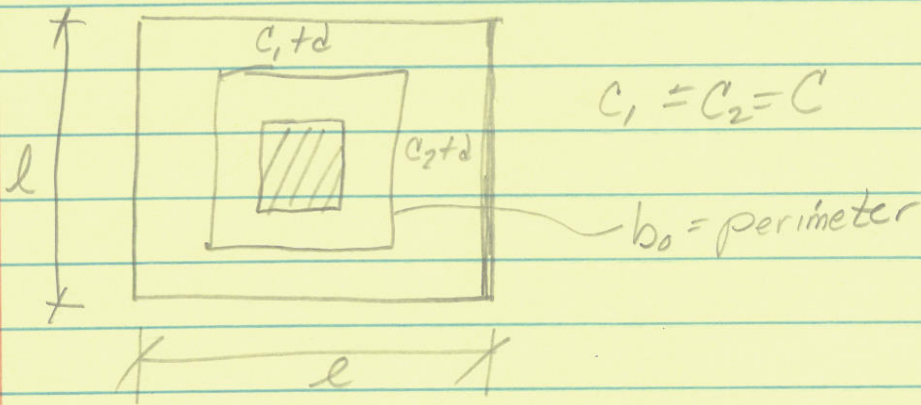
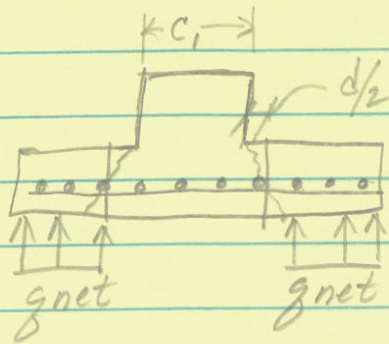
[11.4.5.1]

If $\phi V_c > V_u \rightarrow$ No shear required

If Shear problems

- Increase t_f
- Use Shear reinforcing

Two Way Shear



$$V_u = [l^2 - (c+d)^2] g_{net} (2 + \frac{4}{\beta}) \sqrt{f'_c} b_0 d$$

$\beta = \text{ratio long side to short side}$

$$V_c = \min \left\{ \begin{array}{l} \left(\frac{\alpha_s d}{b_0} + 2 \right) \sqrt{f'_c} b_0 d \\ 4 \sqrt{f'_c} b_0 d \end{array} \right.$$

$\alpha_s = 40$ interior column
 30 edge column
 20 corner column

If $\phi V_c \geq V_u$, no shear reinf. needed

